MMM	MMM	TTTTTTTTTTTTTT	ННН	ннн	RRRRRRRR	RRRR	TTTTTTTTTTTTTT	LLL
MMM	MMM	††††††††††††††††	ННН	ННН	RRRRRRRR		TTTTTTTTTTTTT	
MMM	MMM	ŤŤŤŤŤŤŤŤŤŤŤŤŤŤŤŤŤ	ННН	ннн	RRRRRRR		i i i i i i i i i i i i i i i i i i i	
MMMMMM	MMMMMM	111	ННН	HHH	RRR	RRR	777	
MMMMMM	MMMMMM	+++						FFF
		111	ННН	ннн	RRR	RRR	ŢŢŢ	ŕŕŕ
MMMMMM		!!!	ННН	HHH	RRR	RRR	ŢŢŢ	LLL
	MMM MMM	ŢŢŢ	HHH	HHH	RRR	RRR	TTT	LLL
	MMM MMM	111	HHH	HHH	RRR	RRR	TTT	LLL
MMM	MMM MMM	TTT	HHH	HHH	RRR	RRR	TTT	LLL
MMM	MMM	TTT	нинининини		RRRRRRRR		ŤŤŤ	ĬĬĬ
MMM	MMM	TTT	<b>НИНИНИНИНИ</b>		RRRRRRRR		ŤŤŤ	<i>ו</i> ווֹ דּ
MMM	MMM	ŤŤŤ	<b>НИНИНИНИНИ</b>		RRRRRRRR		ŤŤŤ	iii
MMM	MMM	ŤŤŤ	ННН	ннн	RRR RR		ŤŤŤ	ili
MMM	MMM	ŤŤŤ	нин	ннн	RRR RR		tii	
MMM	MMM	ή††						LLL
		111	HHH	ннн			ŢŢŢ	rrr
MMM	MMM	111	ннн	ННН	RRR	RRR	ŢŢŢ	rrr
MMM	MMM	ŢŢŢ	ННН	HHH	RRR	RRR	ŢŢŢ	LLL
MMM	MMM	TTT	ННН	HHH	RRR	RRR	TTT	LLL
MMM	MMM	TTT	HHH	HHH	RRR	RRR	TTT	
MMM	MMM	TTT	HHH	HHH	RRR	RRR	TTT	
MMM	MMM	111	ннн	HHH	RRR	RRR	ŤŤ	

MT MT MT MT MT

MT MT MT MT MT MT

MM MM MMMM MMMM MMMMM MMMM MM MM MM MM MM	TTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT	HH HHHHHH	DDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDD	\$	NN	000000 000000 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00
LL LL LL LL LL LL LL LL LL LL LL LL LLLL		\$				

Page

floating Point Sine, Cosine and Sincos Functions .TITLE MTHSDSINCOS .IDENT /2-007/ File: MTHDSINCOS.MAR EDIT: JCW2007

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ABSTRACT:

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9

MTH\$DSIN and MTH\$DCOS are functions which return the floating point sine or cosine value of their single precision floating point argument (radians). The call is standard call-by-reference. MTH\$DSIN\_R7 and MTH\$DCOS\_R7 are special routines which are the same as MTH\$D5IN and MTH\$DCOS except a faster non-standard JSB call is used with the argument in RO and no registers are saved.

40: MTH\$DSINCOS is a routine which returns the floating point sine and cosine value of its single precision floating point radian argument. The call is standard call-by-reference. MTH\$DSINCOS\_R7 is a special routine which is the same as MTH\$DSINCOS, except a faster nonstandard JSB call is used with the argument in RO and no registers are saved.

MTH\$DSIND and MTH\$DCOSD are functions which return the floating point sine or cosine value of their single precision floating point argument (degrees). The call is standard call-by-reference. MTH\$DSIND\_R7 and MTH\$DCOSD\_R7 are special routines which are the same as MTH\$DSIND and MTH\$DCOSD except a faster non-standard JSB call is used with the argument in RO and no registers are saved.

MTH\$DSINCOSD is a routine which returns the floating point sine and cosine value of its single precision floating point degree argument. The call is standard call-by-reference. MTH\$DSINCOSD\_R7 is a special ; routine which is the same as MTH\$DSINCOSD, except a faster non-

```
F 12; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 Page 2 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1 (1)
```

```
58
59
             : standard JSB call is used with the argument in RO and no registers
0000
             : are saved.
0000
         60
0000
         61
         62
0000
0000
               VERSION:
0000
         64
ŎŎŎŎ
         65
               HISTORY:
ŎŎŎŎ
               AUTHOR:
         66
0000
         67
                      MARY PAYNE & JUD LEONARD, 25-MAY-78:
                                                                      Version 0
ŎŎŎŎ
         68
0000
         MODIFIED BY:
0000
               1-1 Tryggve Fossum, 28-May-78
0000
VERSION:
                                2
               HISTORY:
               AUTHOR:
                      BOB HANEK, 25-MAY-78:
                                                  Version 2
         80
         81
               Edit history for Version 2
         82
83
84
85
               2-001 - Fixed overflow problem for large radian arguments. RNH 09-Sept-81 2-002 - Included check for A2 = 0 in DSINCOS for small arguments. RNH
               2-003 - Change DSINCOS so that R6/R7 = |X| instead of X. RNH 29-Sep-81 2-004 - Modified Logic for converting reduced accordance for converting reduced accordance.
         86788901234567
999999999
                        Modified logic for converting reduced argument from integer to
                         to floating format to avoid modifying the exponent of a floating
                         point zero. RNH 21-Oct-81
               2-005 - Modified cosine evaluation logic to check the magnitude of YHI
                         instead of YLO. RNH 01-Nov-81
               2-006 - Modified negative argument logic for DSINCOSD to eliminate bug
                         uncovered by FORTRAN QA.
                        Modified REDUCE_LARGE logic to fix bug detected in QAR 896.
                         RNH 14-Jan-82
               2-007 -
                        Corrected the FFS and FFC instructions in REDUCE_LARGE to properly
                         test bits 0 through 20. The loss of accuracy from only testing 20'
         98
                         bits was detected in an SPR. Cleaned up some comments. JCW 8-JUN-84
```

(2)

```
MTHSDSINCOS
2-007
```

```
floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 ECLARATIONS - Declarative Part of Modu 6-SEP-1984 11:22:35
               DECLARATIONS -
                                                                                      [MTHRTL.SRC]MTHDSINCO.MAR; 1
                                           .SBTTL DECLARATIONS
                                                                                Declarative Part of Module
                     ŎŎŎŎ
                             101
                             102
                     0000
                     0000
                                 : INCLUDE FILES:
                                                            MTHJACKET.MAR
                     0000
                             104
                             105
                     0000
                                 : EXTERNAL SYMBOLS:
                     0000
                             106
                     0000
                             107
                                           .DSABL
                     0000
                             108
                                           .EXTRN
                                                   MTHSAL_4_OV_PI
                     0000
                             109
                                           .EXTRN
                                                   MTHSSSIGNAL
                             110
                                                   MTH$K_FLOUNDMAT
                                           .EXTRN
                             111
                                           .EXTRN
                                                   MTH$$JACKET_TST
                     0000
                                 : EQUATED SYMBOLS:
                     0000
                             114
          0000000B
                     0000
                             115
                                                             = ^X0B
                                          X_1_0V_45
                             116
                     0000
                     0000
                             117
                     0000
                                 ; MACROS:
                             118
                     0000
                             119
                     0000
                             120
                                          SSFDEF
                                                                     : Define SF$ (stack frame) symbols
                     0000
                                          $PSLDEF
                                                                      : Define PSL$ symbols
                     0000
                     0000
                                   PSECT DECLARATIONS:
                     0000
                0000000
                             125
                                           .PSECT
                                                   _MTH$CODE
                                                                     PIC, SHR, LONG, EXE, NOWRT
                     0000
                             126
                                                                      ; program section for math routines
                     0000
                             127
                     0000
                                   OWN STORAGE:
                                                   none
                             129
130
                     0000
                     0000
                                 : CONSTANTS:
                             131
132
133
                     0000
                                 D_P1_0V_4:
                     0000
68C2A221 OFDA4049
                     0000
                                           QUAD.
                                                   ^x68C2A2210FDA4049
                                                                              : 0.7853981633974483E+00
                             134
135
                                 D_9_PI_0V_4:
                     0008
                                           QUAD
95DAF665 31D541E2
                     0008
                                                   ^x95DAF66531D541E2
                                                                              : 0.7068583470577035E+01
                             136
137
                                 D_3_PI_OV_4:
                     0010
0E92F999 CBE34116
                                           QUAD
                     0010
                                                   ^x0E92F999CBE34116
                                                                              : 0.2356194490192345E+01
                             138
139
                                 D_5_PI_OV_4:
                     0018
C2F34AA9 53D1417B
                                           .QUAD
                                                   ^xc2f34AA953D1417B
                                                                              : 0.3926990816987242E+01
                                 D_7_PI_OV_4:
                             140
3BAA4DDD EDDF41AF
                                                   ^x3BAA4DDDEDDF41AF
                                                                              : 0.5497787143782138E+01
                             142
                                 D_2_OV_P1:
44156E4E F9834022
                                           .QUAD
                                                    ^x44156E4EF9834022
                                                                              : 0.6366197723675813E+00
                     0030
                     0030
                             145
                                 D_45:
                     0030
00000000 00004334
                                           .QUAD
                             146
                                                    ^x00000000000004334
                                                                              : 0.4500000000000000E+02
                     0038
                             147
                                 D_M45:
00000000 00000334
                                           _QUAD
                                                   ^x0000000000000C334
                                                                               : -.4500000000000000E+02
                     0040
                             149
                                 D_SMALLD:
                     0040
OFBED31E 2EE035E5
                                           QUAD
                                                    ^x0fBED31E2EE035E5
                                                                              : 0.4268868231257969E-06
                     0048
                                 D_1_0V_45:
                             152
153
                     0048
60B6B60B 0B603DB6
                                           QUAD.
                                                    ^x60B6B60B0B603DB6
                                                                              : 0.22222222222222E-01
                                 D_CONVERT:
                     0050
                     0050
9088294E A3513BEF
                                           QUAD.
                                                   ^x9C8B294EA3513BEF
                                                                              : 0.1828292519943295E-02
                                 D_90_0V_PI:
                             155
                     0058
                             156
OFBED31E 2EE042E5
                     0058
                                           .QUAD
                                                    ^x0fBED31E2EE042E5
                                                                              : 0.2864788975654116E+02
```

G 12

OFBED31E	2EE00365	0060 1 0060 1 0068 1	57 D_SMALL 58 59	EST_DEG:	^x0FBED31E2EE00365	; 0.1683771628589691E-36
		0068 1	60 61 PI_OV_2	•		
68C2A221	OFDA40C9	0068 1 0068 1	62 : pi/2	.QUAD	^x68c2a2210FDa40c9	: 0.1570796326794897E+01
03708A2E 44531270	13192303	0070 1 0078 1	64 65	.QUAD	^X03708A2E131923D3 ^X4453127089480766	: 0.5721188726109832E-17 : 0.4335905065061890E-34
68C2A221	OFDA4149	0080 1	66 ; pi 67	.QUAD	*x68C2A2210FDA4149	; 0.3141592653589793E+01
03708A2E 44531270	13192453 894807E6	0090 1	68 69	DAUD.	^x03708A2E13192453 ^x44531270894807E6	: 0.1144237745221966E-16 : 0.8671810130123781E-34
0E92F999 BEB66C2E	CBE34196 D8D6A530	0098 1	70 ; 3*pi/; 71 72	.QUAD .QUAD	^X0E92F999CBE34196 ^XBEB66C2ED8D6A530	: 0.4712388980384690E+01 :3834758505292833E-16
333E0DD4			72 73 74 :2*pi	QUAD.	^x333E0DD4E6F6082C	0.1300771519518567E-33
68C2A221 03708A2E	OFDA41C9 131924D3	0080 1	75 76	.QUAD	^x68C2A2210FDA41C9 ^x03708A2E131924D3	: 0.6283185307179586E+01 : 0.2288475490443933E-16
44531270		0000 1	77 78	.QUAD	^x4453127089480866	: 0.1734362026024756E-33

(4)

6F06EA8A E60A2FFC

00B11EA4 68F6B3D3

F91E4181 FA833770

6ADFF1E4 E9E3BAAA

0190

0198

01A0

01A8

```
; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 DECLARATIONS - Declarative Part of Modu 6-SEP-1984 11:22:35
                                                                                                     VAX/VMS Macro V04-00
                                                                                                     [MTHRTL.SRC]MTHDSINCO.MAR; 1
                                  181
                                                   .SBTTL COEFFICIENT TABLES
                                                                                                       Series Coefficients
                                  182
                         8 jóó
                         0008
                                  185
                         0008
                         0008
                         0008
                                          Polynomial Coefficient tables for arguments in radians
                         0008
                                  188
                         0008
                                  189
                                                            0008
                                  190 COSTBR1:
699DF786 B56AAE47
49E73CCE 74AA320F
                         0008
                                  191
                                                   QUAD.
                         0000
                                  192
                                                  .QUAD
                                  193
CC8A7F10 F27BB593
                         00D8
                                                  .QUAD
B3EDCD6B 0D0038D0
                         00E0
                                  194
                                                  .QUAD
B166B609 0B60BBB6
                         00E8
                                  195
                                                   .QUAD
A99AAAAA AAAA3E2A
                         00F0
                                  196
                                                             ^XA99AAAAAAAAA3E2A
                                                                                               C2 = 0.416666666666643E-01
                                                   .QUAD
                                                                                            FFFFFFFF FFFFFFF
                         00F8
                                  197
                                                             ^YEFFFFFFFFFBFF
                                                   QUAD.
                                                             ^ 000000000004080
0000000 00004680
                         0100
                                   198
                                                                                             QUAD.
            80000008
                         0108
                                       COSLENR1 = .-COSTBR1/8
                                  199
                         0108
                                   200
                                                            ; DCOS coefficients for arguments greater than 1/2

*X699DF786B56AAE47 ; C7 = -.1135212320578394E-10

*X49E73CCE74AA320F ; C6 = 0.2087555514567788E-08

*XCC8A7F10F27BB593 ; C5 = -.2755731286569608E-06

*XB3EDCD6B0D0038D0 ; C4 = 0.2480158728289946E-04

*XB166B6090B60BBB6 ; C3 = -.138888888888888888896E-02
                                       COSTBR2:
                         0108
                                   201
699DF786 B56AAE47
49E73CCE 74AA32OF
CC8A7F10 F27BB593
                                  202
                         0108
                                                   QUAD.
                         0110
                                                   GAUQ.
                         0118
                                   204
                                                   QUAD.
                         0120
0128
0130
0138
B3EDCD6B 0D0038D0
B166B609 0B60BBB6
                                  205
                                                   .QLAD
                                   206
207
208
209
                                                   .QUAD
A99AAAAA AAAA3E2A
                                                                                               \vec{C}^2 = 0.416666666666643E-01
                                                   QUAD.
                                                             ^xa99aaaaaaaa3e2a
F7326202 03392404
E9809A22 4BFDA029
                                                   QUAD.
                                                             ^xf732620203392404
                                                                                               C1 = 0.7156417079102195E-17
                         0140
                                                             ^XE9809A224BFDA029
                                                   QUAD.
                                                                                             : c0 = -.358499999999999999=-19
                                  210
211
212
213
214
215
            00000008
                         0148
                                       COSLENR2 = .-COSTBR2/8
                         0148
                                       SINTBR:
                         0148
                                                               DSIN coefficients
                                                             4 x 2 4 F 1 F 2 B 5 4 C 4 A A C 5 5
24F1F2B5 4C4AAC55
DA66F085 903A3030
                         0148
                                                   QUAD
                                                                                               C7 = -.7577867884012712E-12
                                                                                            : C6 = 0.1605834762322461E-09

: C5 = -.2505210473826733E-07

: C4 = 0.2755731921339017E-05

: C3 = -.1984126984125311E-03

: C2 = 0.83333333333333320E-02
                         0150
                                                             ^XDA66F085903A3030
^X2AF0320D3229B3D7
                                                   .QUAD
2AF0320D 3229B3D7
                         0158
                                                  .QUAD
                                   216
D2FC2984 EF1D3738
                         0160
                                                             ^XD2FC2984EF1D3738
                                                  QUAD.
                         0168
                                   217
3FDEDOOC ODOOBASO
                                                             ^X3FDEDOOCODOOBA50
                                                   .QUAD
                                   218
884D8888 88883D08
                                                             ^x884D88888883D08
                                                   QUAD
                                   219
                         0178
                                                             ^XAAABAAAAAAABF2A
                                                                                             : C1 = -.16666666666667E+00
AAABAAAA AAAABF2A
                                                   .QUAD
                                                                                            \dot{c}0 = -.1879741879570161E-20
4800F1E9 077E9E0E
                         0180
                                                             ^x4800F1E9077E9E0E
                                                   QUAD.
                                  221
222
223
224
225
226
                         0188
            00000008
                                        SINLENR = .-SINTBR/8
                         0188
                         0188
                         0188
                                          Polynomial coefficients for arguments in cycles
                         0188
                                  231
233
233
233
235
236
                         0188
                                        COSTBC1:
                                                            OADSCCAC 2C35ABD9
                         0188
                                                   QUAD.
```

^X6F06EA8AE60A2FFC

^X00B11EA468F6B3D3

^xF91E4181FA833770

^X6ADFF1E4E9E3BAAA

.QUAD

.QUAD

QUAD.

QUAD

C6 = 0.1150049702426300E-09 C5 = -.2461136382637005E-07 C4 = 0.3590860445885820E-05 C3 = -.3259918869266876E-03

```
J 12; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 Page 6 COEFFICIENT TABLES - Series Coefficients 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1 (4
```

```
^XD54E40DAE0F83D81
^X2EF24DF2E9E6BF9D
^XE9809A224BFDA029
                                                                                     : C2 = 0.1585434424381541E-01
: C1 = -.3084251375340425E+00
: C0 = -.3584999999999999E-19
D54E40DA E0F83D81
                                               .QUAD
2EF24DF2 E9E6BF9D
E9809A22 4BFDA029
                                238
239
                       01B8
                                               .QUAD
                       0100
                                               .QUAD
           80000008
                                240 COSLENC1 = .-COSTBC1/8
                       01 C 8
                       0108
                                                       242 COSTBC2:
                       0108
OADSCCAC 2C35ABD9
                       0108
                                              .QUAD
                                244
6F06EA8A E60A2FFC
                       01D0
                                               .QUAD
00B11EA4 68F6B3D3
                       0108
                                245
                                              .QUAD
F91E4181 FA833770
                                246
                       01E0
                                              .QUAD
6ADFF1E4 E9E3BAAA
                       01E8
                                247
                                              .QUAD
                       Ŏ1F0
                                248
D54E40DA E0F83D81
                                              .QUAD
                                249
77916F91 4F32BE6F
                       01F8
                                              .QUAD
E9809A22 4BFDA029
                       0200
                                250
                                              .QUAD
                       0208
           80000008
                                251 COSLENC2 = .-COSTBC2/8
                       0208
                       0208
                                253 SINTBC:
                                                        DSIN coef for arg in cycles

*X86037C402C65A9B6 ; C7 = -.2022531292930000E-13
86037C40 2C65A9B6
D11BCC06 77632DF4
                                              .QUAD
                       0208
                       0210
                                255
                                              QUAD.
                                                        ^XD11BCC0677632DF4
                                                                                        C6 = 0.6948152035052200E-11
                                                                                     \vdots \zeta = -.1757247417617081E-08
0477A15F 83A5B1F1
                       0218
                                256
                                              .QUAD
                                                        ^X0477A15F83A5B1F1
                                                                                     ; C4 = 0.3133616889173253E-06
                       0220
0228
0230
                                                        ^X693342E13C1A35A8
^X5DE873156966B919
693342E1 3C1A35A8
                                              QUAD.
                                                                                     ; \vec{C3} = -.3657620418214640E-04
5DE87315 6966B919
                                258
                                              .QUAD
                                                                                     \ddot{\zeta} = 0.2490394570192716E-02
56C73BAD 35E33C23
                                259
                                              QUAD.
                                                        ^x56C73BAD35E33C23
                                                                                     \ddot{c}_{1} = -.8074551218828078E-01
F296312D 5DE7BEA5
                       0238
                                260
                                              QUAD
                                                        *XF296312D5DE7BEA5
8C232216 FDAA3E10
                       0240
                                               QUAD.
                                                        ^X8C232216FDAA3E10
                                                                                     : CO = 0.3539816339744831E-01
                                261
           00000008
                                262 SINLENC = .-SINTBC/8
                       0248
                                263
                                264
                                265
                                266
                       0248
                                267
                       0248
                                268
                                269
                                    ; Polynomial coefficients for arguments in degrees
                                270
                       0248
                               272 COSDTB2:
273
274
                       0248
                                                        00C69319 09F3856B
                       0248
                                              .QUAD
                                                                                     ; C6 = 0.1667886312398853E-29
; C5 = -.7227873495985315E-24
; C4 = 0.2135494301985905E-18
; C3 = -.3925831985734635E-13
6EB1B88D 50A40F07
                       0250
                                              .QUAD
                                                        ^X6EB1B88D50A40F07
8C1C14B5 B11D985F
                       0258
                                275
                                                        ^x8C1C14B5B11D985F
                                              .QUAD
8EECE026 1D5A217C
                       0560
                                276
                                                        ^X8EECE0261D5A217C
                                               QUAD.
C57ADDE3 CDC2AA30
                       0268
                                277
                                                        ^XC57ADDE3CDC2AA30
                                               QUAD.
                                                                                     (2 = 0.3866323851562972E-08)
(1 = -.1523087098933543E-03)
                                278
279
E39C541E D88B3284
                       0270
                                                        ^xE39C541ED88B3284
                                               .QUAD
FDCCD8AO B50EBA1F
                       0278
                                                        ^XFDCCD8A0B50EBA1F
                                               .QUAD
                       0288
0288
0288
0288
0298
0298
                                280 .QUAD ^X0000000
281 COSDLN2 = .-COSDTB2/8 - 1
00000000 00004080
                                                        ^x0000000000004080
                                                                                      : C0 = 0.10000000000000000000E+01
           00000007
                                283
288
288
288
288
299
293
293
293
                                                       COSDIB1:
00C69319 09F3856B
6EB1888D 50A40F07
                                              .QUAD
                                              .QUAD
8C1C14B5 B11D985F
8EECE026 1D5A217C
C57ADDE3 CDC2AA30
                                              .QUAD
                                               .QUAD
                       02A8
                                               .QUAD
                       02B0
02B8
02C0
02C8
E39C541E D88B3284
EE5FC507 A876B8FD
                                               QUAD.
                                               QUAD
E9809A22 4BFDA029
                                               .QUAD
           0000007
                                    COSDLN1 = .-COSDTB1/8 - 1
```

BDA56DF7 33F0808C 19375C16 08060A3A C2AEE060 B2*B93B5 81336423 53-21CFA B337FD49 B46CA5E1 6B1B5708 6CA72E6D 7BC46CA1 DC10B66D 9C8B294E A3513BEF 00000007	00000000000000000000000000000000000000	297 .QUAD 298 .QUAD 299 .QUAD 300 .QUAD 301 .QLAD	DSIN coefficients AXBDAS6DF733F0808C AX19375C1608060A3A AXC2AEE060B88B93B5 AX8133642353021CFA AXB337FD49B46CA5E1 AX6B1B57086CA72E6D AX7BC46CA1DC10B66D AX9C8B294EA3513BEF B/8 - 1	: C7 =3218900432111067E-38 : C6 = 0.2239270886637075E-32 : C5 =1146820010579771E-26 : C4 = 0.4141267415665013E-21 : C3 =9788384861609472E-16 : C2 = 0.1349601623163253E-10 : C1 =8860961557012980E-06 : C0 = 0.1828292519943296E-02
--	--	---	---	--

```
Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 ITH$DSINCOS - Radian arguments 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
       MTHSDSINCOS - Radian arguments
              0308
0308
0308
                        306
307
308
309
                                          .SBTTL MTH$DSINCOS
                                                                                       Radian arguments
              0308
              0308
                        310
                              : FUNCTIONAL DESCRIPTION:
              0308
                        311
              0308
                                The DSIN, DCOS and DSINCOS routines are based on octant reduction. Given an
              0308
0308
0308
0308
0308
                                argument, x, it is written in the form
                                                x = I1*(2*pi) + I*(pi/4) + Y1,
                         315
                                where I1 and I are integers, 0 = < I < 8 and 0 = < Y1 < pi/4. Since DSIN and DCOS have a period of 2*pi it follows that
              0308
                        319
                        320
321
322
323
              0308
                                                DSIN(x) = DSIN(I*(pi/4) + Y1)) \text{ and } DCOS(x) = DCOS(I*(pi/4) + Y1)).
              0308
              0308
              0308
                                Using the trigonometric identities for the sum and difference of two angles,
              0308
                                the following table can be generated:
                        325
326
327
              0308
              0308
                                         If I =
                                                                   then DSIN(x) =
                                                                                                             and DCOS(x) =
              0308
              0308
                                            0
                                                                     DSIN(Y1)
                                                                                                                DCOS(Y1)
              0308
                                                                     DCOS(pi/4-Y1)
DCOS(Y1)
                                                                                                                DSIN(pi/4-Y1)
              0308
                        330
                                                                                                               -DSIN(Y1)
              0308
                        331
                                                                    DŠÍN(pi/4-Y1)
-DSÍN(Y1)
                                                                                                               -DCOS(pi/4-Y1)
              0308
                                                                                                               -DCOS(Y1)
              0308
                                                                    -DCOS(pi/4-Y1)
-DCOS(Y1)
                                                                                                               -DSIN(pi/4-Y1)
              0308
                                            67
                                                                                                                DSIN(Y1)
              0308
                        335
                                                                    -DSIN(pi/4-Y1)
                                                                                                                DCOS(pi/4-Y1)
              0308
                        336
                                Let Y be defined as Y = Y1 if I is even and Y = pi/4 - Y1, if I is odd, then each entry of the above table is of the for +/-DSIN(Y) or +/-DCOS(Y). Based on the above remarks, the DSIN, DCOS and DSINCOS routines process the input argument x, to obtain I and Y, and based on I selects a suitable polynomial
                        337
              0308
              0308
                        338
              0308
                        339
              0308
              0308
                        341
                                approximation, p(Y) to evaluate the desired fuction.
              0308
              0308
                        343
              0308
                        344
                                INPUT PARAMETERS:
              0308
                        345
00000004
              0308
                        346
                                         LONG
00000004
              0308
                        347
                                                   = 1*LONG
                                                                           ; x is input angle in radians
00000008
              0308
                        348
                                         sine = 2*LONG
cosine = 3*LONG
                                                                           ; sine is DSIN(x)
              0308
                        349
00000000
                                                                           : cosine is DCOS(x)
              0308
                        350
```

MT

Page

(5)

L 12

9 (7)

		; FL MTH\$	oating Point DSINCOS - Ra	M 12 t Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 Page adian arguments 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
			0308 352 0308 353 0308 354 0308 355	Return sine and cosine of argument
		00F C	0308 356 0308 357 0308 358 0308 359 030A 360	.ENTRY MTH\$DSINCOS, ^M <r2, r3,="" r4,="" r5,="" r6,r7=""></r2,>
			0308 359 030A 360 030A 361 030A	MTH\$FLAG_JACKET
6D	0000000°GF	9E	0.50.	MOVAB G^MTH\$\$JACKET_HND, (FP) ; set handler address to jacket ; handler
	50 04 BC 00000390'EF 08 BC 50 0C BC 52	70 16 70 70 04	0311 0311 0311 0311 0311 0311 0315 0315	MOVD ax(AP), RO JSB MTH\$DSINCOS_R7 MOVQ RO, asine(AP) MOVQ R2, acosine(AP) RET
			031F 366 0323 367 0324 368 0324 370 0324 371 0324 373 0324 373 0324 375 0324 376 0324 377 0324 377 0324 377	.SBTTL MTH\$DSIN  Return sine of argument
		00F C	0324 378 0324 378 0326 379	.ENTRY MTH\$DSIN, ^M <r2, r3,="" r4,="" r5,="" r6,="" r7=""></r2,>
			0326 380 0326	MTH\$FLAG_JACKET
6D	0000000°GF	9E	0326 032D 032D 032D	<pre>MOVAB G^MTH\$\$JACKET_HND, (FP)</pre>
	50 04 BC 00000493'EF	70 16 04	032D 381 032D 382 0331 383 0337 384 0338 385 0338 386 0338 388 0338 389 0338 391 0338 391 0338 391 0338 393 0338 395 0338 395 0338 397 033A 397	MOVD @x(AP), RO JSB MTH\$DSIN_R7 RET
			0338 387 0338 388 0338 389	.SBTTL MTH\$DCOS
			0338 391 0338 392 0338 393	Return cosine of argument
		00F C	0338 394 0338 395 033A 396	.ENTRY MTH\$DCOS, ^M <r2, r3,="" r4,="" r5,="" r6,="" r7=""></r2,>
			033A 397 033A	MTH\$FLAG_JACKET

MTHSDSINCOS 2-007			, F1	oating DCOS	Point Si	ne, Cosine	N 12 and Sincos	16-SEP-1984 6-SEP-1984	01:20: <b>38</b> 11:22:35	VAX/VMS Macro VO4-00 [MTHRTL.SRC]MTHDSINCO.MAR;1	Page	10 (7)
	60	0000000°GF	9E	033A 0341 0341 0341		MOVAB	G^MTH\$\$J/	ACKET_HND, (I	FP) ; set ; hand	handler address to jacket Ner		
		50 04 BC 0000051A'EF	70 16 04	0341 0341 0345 0348 0340	398 399 400 401 402	MOVD JSB RET	ax(AP), F MTH\$DCOS	RO _R7				

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```
; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 MTH$DSINCOSD - Degrees 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
       MTH$DSINCOSD - Degrees
                                                                                                                                               (8)
                                         .SBTTL MTH$DSINCOSD
                                                                                     Degrees
              034C
                        405
              0340
                        406
              0340
                       407
                               FUNCTIONAL DESCRIPTION:
              034C
                       409
              0340
                       419
                                The DSIND, DCOSD and DSINCOSD routines are based on octant reduction. Given
                       411
                                an argument, x, it is written in the form
                       412
                                               x = 11 + 360 + 1 + 45 + 41
                        414
                                where I1 and I are integers, 0 =< I < 8 and 0 =< Y1 < 45. Since DSIND and DCOSD have a period of 360 it follows that
                       415
                        416
                        417
                                               DSIND(x) = DSIND(1*45 + Y1) and DCOSD(x) = DCOSD(1*45 + Y1).
                       418
                       419
                                Using the trigonometric identities for the sum and difference of two angles,
                       423
424
425
426
                               the following table can be generated:
                                        If I =
                                                                                                             and DCOSD(x) =
                                                                  then DSIND(x) =
                                           0
                                                                    DSIND(Y1)
                                                                                                                DCOSD(Y1)
                                                                    DCOSD(45-Y1)
                                                                                                                DSIND (45-Y1)
                                                                    DCOSD(Y1)
                                                                                                              -DSIND(Y1)
                                                                    DSIND (45-Y1)
                                                                                                              -DCOSD(45-Y1)
                                                                   -DSIND(Y1)
                        430
                                                                                                              -DCOSD(Y1)
                                                                   -DCOSD(45-Y1)
                                                                                                              -DSIND(45-Y1)
                                                                   -DCOSD(Y1)
                                                                                                               DSIND(Y1)
                                           6
                       433
                                                                   -DSIND(45-Y1)
                                                                                                                DCOS (45-Y1)
                               Let Y be defined as Y = Y1 if I is even and Y = 45 - Y1, if I is odd, then each entry of the above table is of the for +/-DSIN(Y) or +/-DCOS(Y). Based on the above remarks, the DSIND, DCOSD and DSINCOSD routines process the input argument x, to obtain I and Y, and based on I selects a suitable polynomial
              034C
                       435
              034C
                       437
                       439
                               approximation, p(Y), to evaluate the desired fuction.
              034C
              034C
                       441
                       442
00000004
             0340
                                        LONG = 4
                                        sind = 2*LONG
cosd = 3*LONG
80000008
             034C
0000000
             034C
              034C
```

B 13

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?-007							nd Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 Page 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1	(
			OOF C	034E 034E 034E	447 448		MTH\$DSINCOSD	
				034E 034E	449	MTHSFLA	G_JACKET	
	6D	0000000°GF	9E	034E 0355 0355 0355		MOVAB	G^MTH\$\$JACKET_HND, (FP) ; set handler address to jacket ; handler	
		50 04 BC 000005A8'EF 08 BC 50 0C BC 52	70 16 70 70	034E 0355 0355 0355 0355 0355 0367 0367 0368	450 451 452 453 455 455 457 458 459	MOVD JSB MOVQ MOVQ	ax(AP), RO MTH\$DSINCOSD_R7 RO, asind(AP) R2, acosd(AP)	
			04	0368	456 457 458	RET		
			00F C	0368 0368	460	.ENTRY	MTH\$DSIND	
				036A 036A	461 462	MTH\$FLA	G_JACKET	
	6D	0000000'GF	9E	036A 036A 0371 0371 0371		MOVAB	G^MTH\$\$JACKET_HND, (FP) ; set handler address to jacket ; handler	
		50 04 BC 00000603'EF	70 16	0371 0371 0375 0378	463 464 465 46 <u>6</u>	MOVD JSB	ax(AP), RO MTH\$DSIND_R7	
			04	037B 037C 037C	467 468 469 470	RET		
			00F C	037C 037C 037E	4/1	.ENTRY	MTH\$DCOSD	
				037E	472 473	MTHSFLA	G_JACKET	
	6D	0000000°GF	9E	037E 037E 0385 0385		MOVAB	G^MTH\$\$JACKET_HND, (FP) ; set handler address to jacket ; handler	
		50 04 BC 00000661 EF	70 16	0385 0385 0385 0385 0385 0386 0386	474 475 476	MOVD JSB	ax(AP), RO MTH\$DCOSD_R7	
			04	038F 038F 0390	477 478 479	RET		

```
Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 TH$DSINCOS_R7 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
                 MTHSDSINCOS_R7
                                                                                                                                         (10)
                                               .SBTTL MTH$DSINCOS_R7
                       0390
                       0390
                                       This routine computes the DSIN and DCOS of the G-format value of RO/R1. The
                                484
                       0390
                                        computation is performed one of three ways depending on the size of the
                       0390
                                        input argument, X:
                       0390
                                486
487
                       0390

    If 'X' < pi/4, then X is used directly in polynomial approximation</li>

                       0390
                                                   of DSIN and DCOS.
                       0390
                                489
                                               2) If pi/4 =< |xi < 9*pi/4, then the subroutine REDUCE_MEDIUM is called
                       0390
                                490
                                                   to reduce the argument to an equivalent argument in radians, Y, and
                       0390
                                491
                                                   the octant, I, containing the argument. Y is then evaluated in two polynomials chosen as a function of I, to compute DSIN(X) and DCOS(X).
                       0390
                       0390
                                               3) If 9*pi/4 =< |X|, then the subroutine REDUCE_LARGE is called to
                                                   reduce the argument to an equivalent argument in cycles, Y, and the octant, I, contanining the argument. Y is then evaluated in two polynomials chosen as a function of I, to compute DSIN(X) and DCOS(X).
                       0390
                       0390
                                495
                       0390
                                496 :
                       0390
                                497
                                478 MTH$DSINCOS_R7::
                       0390
                                                        RO, R6
POS SINCOS
SINCOS
      56
            50
                       0390
                                                                                         R6 = X
                  18
                       0393
                                500
                                               BGEQ
 0000039F
                       0395
            'EF
                  16
                                501
                                                                                         RO/R1 = DSIN(:X!), R2/R3 = DCOS(X)
                                               JSB
            50
                  72
05
                                502
503
                       039B
      50
                                               MNEGD
                                                         RO. RO
                                                                                         RO/R1 = DSIN(X)
                       039E
                                               RSB
                       039F
                                504
                                505 SINCOS:
                       039F
56
      8000 8F
                       039F
                                506
                                                         #^x8000, R6
                  AA
                                               BICW
                                                                                       : R6/R7 = XX
                                507
                       03A4
                                     POS_SINCOS:
                                                         D_PI_OV_4, R6
SMALE_SINCOS
D_9_PI_OV_4, R6
1$
                       03A4
                                508
56
      FC58 CF
                                               CMPD
                                                                                       : Compare pi/4 with IXI
                  14
                       03A9
                                509
                                               BGTR
                                                                                         No argument reduction is necessary
56
      FC59
            CF
                  71
                       03AB
                                510
                                               CMPD
                                                                                       : Compare 9*pi/4 with IXI
            03
                  18
                       0380
                                511
                                               BGEQ
                                512
513
         00B4
                  31
                       03B2
                                               BRW
                                                         LARGE_SINCOS
                                                                                       ; Use special logic for IX: > 9*pi/4
                       03B5
                       0385
                                514
                                        pi/4 = < |X| < 9*pi/4
                       03B5
                                515
                                516
                       03B5
                                517 1s:
 0000069A'EF
                       03B5
                  16
                                               JSB
                                                         REDUCE_MEDIUM
                                                                                         Medium argument reduction routine
                       03BB
                                518
                                                                                         R4/R7 = Y = reduced argument
                       03BB
                                519
                                                                                         R2 = octant
      7E
7E
            54
56
                  70
                       03BB
                                520
                                               DVOM
                                                         R4, -(SP)
                                                                                         Save reduced argument on stack
                                521
522
523
524
526
                  7D
                       03BE
                                                         R6, -(SP)
                                               PVOM
                       0301
                  DD
                                               PUSHL
                                                         R2
                                                                                         Save octant bits on stack
 00000535
                  16
                       0303
                                               JSB
                                                         M_COS
                                                                                         RO/R1 = DCOS(X)
      52
56
                  DO
70
                                                         (5P)+, R2
                       0309
                                               MOVL
                                                                                         R2 = Octant bits
                                                         (SP)+, R6
            8E
                       0300
                                               MOVQ
                                                         (SP)+, R4
RO, -(SP)
M_SIN
      54
            8E
                  7D
                       03CF
                                                                                         R4/R7 - reduced argument
                                               MOVQ
            50
                  70
                       0302
                                527
                                               MOVQ
                                                                                         Save DCOS(X) on stack
 000004BA
            'EF
                  16
                       03D5
                                528
                                               JSB
                                                                                         kO/R1 = DSIN(X)
                                529
530
                  7D
05
                                                                                         R2/R3 = DCOS(X)
      52
                       03DB
                                                         (5P)+, R2
                                               MOVQ
                       03DE
                                               RSB
                       03DF
                                532
533
534
535
536
537
                       03DF
                                       Logic for small arguments. IXI < pi/4.
                       03DF
                       03DF
                       03DF
                                    SMALL_SINCOS:
                                                         #^x4000, R6
                       03DF
56
            8f
                  B1
                                               CMPW
                                                                                       ; Compare 1/2 with IXI
            33
                   15
                       03E4
                                               BLEQ
                                                                                       ; Sufficent overghang not available
```

D 13

	E 13				
; Floating Point Sine, MTH\$DSINCOS_R7	Cosine and Sincos	16-SEP-1984 01:20:38 6-SEP-1984 11:22:35	VAX/VMS Macro VO4-00 [MTHRTL.SRC]MTHDSINCO.MAR;1	Page	14 (10)

FCCE FD42		3280 56 7E 07 54 6E 07 50 52 8000	56 54 56 55 56 56 8E	B1 185 775 775 775 60 705 708	03EB 03SED 03FF4 03FFA 03FFA 0406 0406 0410 0410	890123456789012 555555555555555555555555555555555555	15:	CMPW BGEQ MULD3 MOVQ POLYD MOVQ POLYD MULD ADDD MOVQ RSB		Compare with 2^-28  No polynomial evaluation is needed R4/R5 = X*X  Put X*X on stack  R0/R1 = DCOS(X)  R4/R5 = X*X  Save DCOS(X) on stack  R0/R1 = q(X^2)  R0/R1 = X*q(X^2)  R0/R1 = DSIN(X)  R2/R3 = DCOS(X)  R2/R3 = 1.0 = DCOS(X)  R0/R1 = ix:
FCE2 55	54 CF FFF	56 7E 07 54	564 554 555 554 555 554	65 7D 75 7D CA 63 61	0413 0418 0419 0419 0419 0410 0420 0426 0429 0430	55555555555555555555555555555555555555	2\$:	MULD3 MOVQ POLYD MOVQ BICL SUBD3		
	7E 52 52 54	54 52 0080	56 8E 08 8F	61 643 626 642 627 70	0434 0438 043B 043D 0442 0445 0445 0445	563 5645 5667 5667 5667 5670	<b>3\$</b> :	ADDD3 MULD BEQL SUBW SUBD MULD SUBW SUBD SUBD SUBD	R6, R4, R2 (SP)+, R2 3\$ #^X80, R2 R2, R0 R4, R4 #^X80, R4 #1, R4 R4, R0	R4/R5 = X^2 Save X^2 R0/R1 = Q(Y^2) R4/R5 = X R4/R5 = XHI (SP) = XLO R2/R3 = X + XHI R2/R3 = XLO*(X + XHI) = A2 Check for A2 = O R2/R3 = A2/2 R0/R1 = Q(Y^2) - A2/2 R4/R5 = XHI^2 R4/R5 = XHI^2/2 R4/R5 = XHI^2/2 - 1 R0/R1 = DCOS(X) R2/R3 = X^2
FCE9	CF	50 52 6E 07 50 50	524 558 558 5555 5555 8	7D 75 64 60	0453 0456 0459 0457 0462 0465 0468 0469	571 572 573 574 575 576 577 578 579		MOVQ MOVQ POLYD MULD ADDD MOVQ RSB	R4, R0 (SP), R2 R0, (SP) R2, #SINLENR-1, SINTBR R6, R0 R6, R0 (SP)+, R2	R2/R3 = X^2 Save DCOS(X) R0/R1 = Q(X^2) R0/R1 = X*Q(X^2) R0/R1 = DSIN(X) R2/R3 = DCOS(X)
		00718		16	0469 0469 046F	580 581	LARGE_S	JSB	REDUCE_LARGE :	R4/R7 = reduced argument (in cycles) R2 = octant bits
	000	7E 7E 0057C' 54 56 52 7E 004EE'	52 554 E8E 88E 88E 88E 88E	DD 7D 7D 16 7D 7D 7D 16 7D	046F 0471 0474 0477 0470 0480 0483 0486 0489 0489	55555555555555555555555555555555555555		PUSHL MOVQ JSB MOVQ MOVQ MOVL MOVQ JSB MOVQ RSB	R2 R6, -(SP) R4, -(SP) L_COS (SP)+, R4 (SP)+, R6 (SP)+, R2 R0, -(SP) L_SIN (SP)+, R2	Save octant bits on stack Save reduced argument on stack RO/R1 = DCOS(X) Reduced argument in R4/R7 R2 = octant bits R2/R3 = DCOS(X) RO/R1 = DSIN(X) R2/R3 = DCOS(X)

(11)

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; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 MTH$DSIN_R7 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
                                    595
                                                     .SBTTL MTHSDSIN R7
                          0493
                                    596
                                    597
                          0493
                                            This routine computes the DSIN of the G-format value of RO/R1. The
                                    598
                                            computation is performed one of three ways depending on the size of the
                                    599
                                            input argument, X:
                                    600
                                    601
                                                    1) If |X| < pi/4, then X is used directly in a polynomial approximation
                                    602
                                                     2) If pi/4 =< ixi < 9*pi/4, then the subroutine REDUCE_MEDIUM is called</p>
                                                    to reduce the argument to an equivalent argument in radians, Y, and the octant, I, containing the argument. Y is then evaluated in a polynomial chosen as a function of I to compute DSIN(X).

3) If 9*pi/4 =< :X;, then the subroutine REDUCE LARGE is called to reduce the argument to an equivalent argument in cycles, Y, and the
                                    604
                                    605
                                    606
                                    607
                          0493
                                    608
                                                        octant, I, contanining the argument. Y is then evaluated in a polynomial chosen as a function of I to compute DSIN(X).
                          0493
                                    609
                          0493
                                    610
                          0493
                                    611
                                   612
                                         MTH$DSIN_R7:: TSTD
                          0493
              50
                          0493
                                                                                                   Check the sign of RO
                     18
                          0495
                                    614
                                                               POS_SIN
                                                     BGEQ
                    16
72
35
 000004A1'EF
                          0497
                                    615
                                                                SIN
                                                                                                    RO/R1 = DSIN(:X:)
                                                     JSB
       50
                          049D
                                    616
                                                     MNEGD
                                                                RO, RO
                                                                                                 : RO/R1 = DSIN(X)
                                   617
                          04A0
                                                     RSB
                          04A1
                                    618
                          04A1
                                   619
                                         SIN:
50
       8000 8F
                                                     BICW
                                                                #^x8000, RO
                    AA
                          04A1
                                    620
                                                                                                 : RC/R1 = |X|
                                   621
622
623
                          04A6
                                         POS_SIN:
                                                               D_PI_OV_4, RO
SMALE_SIN
D_9_PI_OV_4, RO
LARGE_SIN
50
       fB56 CF
                    71
                          04A6
                                                     CMPD
                                                                                                   Compare pi/4 with IX:
                                                    BGTR
                    14
                          04AB
                                                                                                    No argument reduction is necessary
50
       FB57
             ČF
                    71
                                   624
                          04AD
                                                     CMPD
                                                                                                   Compare 9*pi/4 with IX1
                    19
                          04B2
                                                                                                  : Use special logic for IXI > 9*pi/4
                                                    BLSS
                                   626
627
                          0484
                          04B4
                                             pi/4 = < |X| < 9*pi/4
                          04B4
                                   628
                          04B4
                                   629
                                   630
631
632
633 M_S
634
635 1$:
 0000069A'EF
                          04B4
                    16
                                                    JSB
                                                               REDUCE_MEDIUM
                                                                                                    Medium argument reduction routine
                          04BA
                                                                                                    R4/R7 = Y^{-} = reduced argument
                          04BA
                                                                                                    R2 = octant
07
      01
             52
                          04BA
                    8F
                                         M_SIN:
                                                    CASEB
                                                               R2, #1, #7
                                                                                                   Branch to one of four polynomial
                          04BE
                                                                                                        evaluations depending on the
                                                               P_COS_R-1$
P_COS_R-1$
N_SIN_R-1$
N_SIN_R-1$
N_COS_R-1$
N_COS_R-1$
P_SIN_R-1$
                  05B7
                          04BE
                                                     . WORD
                  05B7'
                          0400
                                                     . WORD
                 0653'
0653'
0602'
                                                     .WORD
                                   638
639
                                                     .WORD
                          0466
                  0602
                                    64C
                                                     . WORD
                 ٥٥٠٥٠ .
                                    641
                                                     . WORD
                  065D'
                                   642
                                                                P_SIN_R-1$
                                                     .WORD
                                                                                                        octant bits.
                                    645
                                         ; Logic for small arguments. | X| < pi/4.
                                   646
                          04CE
                                         SMALL_SIN:
                                    648
                          04CE
04D3
50
                                                    CMPW
                                                               #^x3280, RO
       3280
                                    649
                                                                                                   Compare with 2^-28
                                                                                                   No polynomial evaluation is needed R6/R7 = X
                     18
                                    650
                                                    BGEQ
                                                                1$
              50
                     7Ď
                                                               RO. R6
       56
                          0405
                                    651
                                                    MOVQ
```

F 13

07CB1

0518

051A

686

687

.WORD

UNFL -1\$

```
; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 MTH$DSIN_R7 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
                            64
75
64
60
05
                                 04D8
04DB
04E1
04E4
04E7
                                           652
653
654
655
              50
07
50
50
                     50
50
56
56
                                                            MULD
                                                                        RO,RO
                                                                                                            RO/R1 = X*X
FC67 CF
                                                                                                            RO/R1 = q(x^2)

RO/R1 = x + q(x^2)
                                                                        RO, #SINLENR-1, SINTBR
                                                            POLYD
                                                                       R6, R0
R6, R0
                                                            MULD
                                                            ADDD
                                                                                                            RO/R1 = DSIN(X)
                                           656 1$:
                                                            RSB
                                  04E8
                                           658
                                 04E8
04EE
04EE
04F0
                                           659 LARGE_SIN:
        00000718'EF
                                           660
                                                            JSB
                                                                        REDUCE_LARGE
                                                                                                          ; R4/R7 = reduced argument (in cycles)
                                           662 L_SIN: ISTL
                                                                                                          ; R2 = octant bits
                     54
14
                            D5
13
                                                                                                         ; Check for degenerate case
                                                                       DEGENERATE_CASE_SIN
                                  04F2
                                           664
       07
                            8F
                                 04F2
              00
                     52
                                           665
                                                            CASEB
                                                                        R2, #0, #7
                                  04F6
                                           666
                                                                       P_SIN_C-1$
P_COS_C-1$
P_COS_C-1$
P_SIN_C-1$
N_SIN_C-1$
N_COS_C-1$
N_COS_C-1$
N_SIN_C-1$
                                           667 15:
                                                             .WORD
                         06E4'
                                 04F6
                                                             .WORD
                         0640' 04F8
                                           668
                                           669
670
                                                             .WORD
                         0640' 04FA
                                                             .WORD
                         06E4' 04FC
                         06DA' 04FE
                                                             .WORD
                                 0500
                                                             .WORD
                         0688
                                                             .WORD
                         06881
                         06DA'
                                                             .WORD
                                  0506
                                           675
                                                 DEGENERATE_CASE_SIN:
                                  0506
                           8A
9C
8F
                                                                       N1, R2
N-1, R2, R2
R2, N0, N3
                                           679
                                 0506
              52
                                                            BICB
                                                                                                         ; Compute index as (R2 - 1)/2
                                 0509
050E
0512
0512
0514
         52 
   52
                FF 8F
                                           680
                                                            ROTL
             00
                                           681
                                                            CASEB
                                           682
683 1$:
                                                                       P_ONE-1$
UNFL -1$
                         078B'
                                                             .WORD
                         07CB1
                                           684
                                                             . WORD
                         07BF 1
                                 0516
                                                                       N_ONE-1$
                                           685
                                                             .WORD
```

G 13

50

07

50

54

50

FB57 CF

50

50 07

50

00000718'EF

80

0572 0575

0576 0576

0576

0576

16

740 25:

744 LARGE\_COS: 745 JS

741

742

01

; RO/R1 = 1.0 = DCOS(X)

; R4/R7 = reduced argument (in cycles)

#1.0, RO

REDUCE\_LARGE

MOVD

RSB

JSB

```
746
747
748
749
750
751
752
753
754
755
756
757
758
759
760
                                                                                                                                ; R2 = octant bits
; Check for degenerate case
                                                                        TSTL
                                13
                                                                        BEQL
                                                                                      DEGENERATE_CASE_COS
                                                                                     R2, #0, #7
P_COS_C-1$
P_SIN_C-1$
N_SIN_C-1$
N_COS_C-1$
N_COS_C-1$
N_SIN_C-1$
P_SIN_C-1$
P_SIN_C-1$
      07
              00
                                                                        CASEB
                                                                         .WORD
                                                                         .WORD
                                                                         .WORD
                                                                         .WORD
                                                                         .WORD
                                                                         . WORD
                                                                         .WORD
                                                                         .WORD
                                       0594
                                       0594
                                                   760
                                       0594
                                                   761 DEGENERATE_CASE_COS:
                                                   762
763
764
765
                                       0594
52 52 52 FF 8F
00 52
                                                                                      N1. R2
N-1, R2, R2
R2, N0, N3
                               8A
9C
8F
                                       0594
                                                                        BICB
                                                                                                                              : Compute index as (R2 - 1)/2
                                      0597
0590
                                                                        ROTL
                                                                        CASEB
                            05A0
073D' 05A0
0731' 05A2
073D' 05A4
072D' 05A6
05A8
                                                   766
767 1$:
                                                                        .WORD
                                                                                      UNFL -1$
                                                   768
769
770
                                                                        .WORD
                                                                                      N_ONE-1$
                                                                                      UNFL -1$
                                                                         .WORD
                                                                                      P_ONE-1$
                                                                        . WORD
```

0602

RSB

```
; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00
MTH$DSINCOSD_R7 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
                 MTHSDSINCOSD_R7
                                                                                                                                         (14)
                                               .SBTTL MTH$DSINCOSD_R7
                       05A8
                                774
                       05A8
                                775
                                       This routine computes the DSIND and DCOSD of the D-format value of RO/R1.
                                776
777
                       ŎŠAŠ
                                       The computation is performed one of two ways depending on the size of the
                       05A8
                                       input argument, X:
                       05A8
                                778
                                779
                       05A8
                                               1) If |X| < 45, then X is used directly in polynomial approximation
                                                  of DSIND and DCOSD.
                       05A8
                                780
                                                  If 45 =< |x|, then the subroutine REDUCE_DEGREES is called to reduce the argument to an equivalent argument in degrees, Y, and the
                       05A8
                                781
                                782
783
                       05A8
                       05A8
                                                  octant, I, containing the argument. Y is then evaluated in two polynomials chosen as a function of I, to compute DSIND(X) and
                       05A8
                                784
                       05A8
                                785
                                                   DCOSD(X).
                                786
                       05A8
                                787 MTH$DSINCOSD_R7::
                       05A8
            50
                       05A8
                                788
                                               TSTD
                                                        R0
            OF.
                  18
                       05AA
                                789
                                               BGEQ
                                                         SINCOSD
     8000 BF
                                790
                  AA
                       05AC
                                               BICW
                                                         #^x8000, RO
                                                                                         RO/R1 = IXI
 000005BB'EF
                                791
                  16
                       05B1
                                               JSB
                                                                                         RO/R1 = DSIND(:X:)
                                                         SINCOSD
                                792
793
                       05B7
                                                                                         R2/R3 = DCOSD(|X|)
                  72
05
            50
      50
                       05B7
                                               MNEGD
                                                        RO, RO
                                                                                       : RO/R1= -DSIND(|X|)
                       05BA
                                794
                                               RSB
                       0588
                                795
                                796 SINCOSD:
                       05BB
                                797
     FA71 CF
                       0588
0500
0502
0508
0508
0508
0503
0503
                                               CMPD
50
                                                        D_45, RO
                                                                                         Compare 45 to IXI
                                798
                                                         SMALL SINCOSD
                                               BGTR
                                                                                         special processing for small arg
 000009CB'EF
                                799
                  16
                                                         REDUCE_DEGREES
                                               JSB
                                                                                         R6/R7 = reduced argument
                                800
                                                                                         R3 = octant
      7E
                                801
                                               MOVQ
                                                         R6, -(SP)
                                                                                         Save reduced and
                                802
803
                  DD
                                               PUSHL
                                                        R3
                                                                                         Save octant bits
                                                        EVAL COSD
(SP) +, R3
 00000675'EF
                  16
                                               JSB
                                                                                         RO/R1 = DCOSD(Y)
            8E
                  DŌ
                                804
                                               MOVL
                                                                                         R3 = octant bits
                                                        (SP), R6
RO, (SP)
EVAL SIND
(SP)+, R2
                                                                                         R6/R7 = reduced argument
      56
                  ŽĎ.
            6Ē
                                805
                                               MOVQ
                       0509
            50
                  7D
                                806
                                               MOVQ
                                                                                         Save DCOSD(Y)
                                807
 00000623'EF
                       05DC
                  16
                                               JSB
                                                                                         RO/R1 = DSIND(Y)
                       05E2
05E5
      52
                  7D
                                808
                                               MOVQ
                                                                                         R2/R3 = DCOSD(Y)
                  05
                                809
                                               RSB
                       05E6
                                810
                       05E6
                               812
813
                                    SMALL_SINCOSD:
                       05E6
                                                        #16, SP
RO, (SP)
                       05E6
            10
                                               SUBL
                                                                                       ; Allocate 4 longwords on stack
                  ŽD
                                814
                       05E9
            50
                                               MOVQ
                                                                                         Save argument
 00000689'EF
                                815
                  16
                       05EC
                                                         SMALL_COSD
                                               JSB
                                                                                         RO/R1 = DCOSD(x)
 08 AE
50
                                                        RO. 8(SP)
            50
                  7D
                       05F2
                                816
                                               MOVQ
                                                                                         Save DCOSD(:X:)
                                                        (SP)+, RO
                  70
                       05F6
                                817
                                                                                        RO/R1 = argument
RO/R1 = DSIND(X)
                                               MOVQ
 00000637
           'EF
                  16
                       05F9
                                818
                                               JSB
                                                        SMALL_SIND
                                819
      52
                  7D
                       05FF
                                               MOVQ
                                                         (SP)+7R2
                                                                                         R2/R3 = DCOSD(1X1)
```

J 13

```
K 13
  floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 TH$DSIND_R7 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
MTHSDSIND R7
      0603
0603
              823
823
825
826
827
                              .SBTTL MTH$DSIND_R7
      0603
                      This routine computes the DSIND of the D-format value of RO/R1. The
      0603
                      computation is performed one of two ways depending on the size of the input
      0603
                      argument, X:
```

```
0603
                                                1) If |X| < 45, then X is used directly in polynomial approximation
                        0603
                                                2) If 45 =< |x|, then the subroutine REDUCE_DEGREES is called to reduce
                                 831
                                                    the argument to an equivalent argument in degrees, Y, and the
                                                    octant, I, containing the argument. Y is then evaluated in two polynomials chosen as a function of I, to compute DSIND(X).
                                     MTH$DSIND_R7::
                                 835
                        0603
                                 836
            50
                        0603
                                                                                           RO/R1 = X
                                                          R0
                   18
            ÔF
                        0605
                                 837
                                                          POS_SIND
                                                BGEQ
                   16
72
05
 00000611'EF
                        0607
                                 838
                                                          NEG_SIND
RO, RO
                                                                                           RO/R1 = DSIND(:X:)
                                                JSB
      50
            50
                        060D
                                 839
                                                MNEGD
                                                                                           RO/R1 = -DSIND(|X|)
                        0610
                                 840
                                                RSB
                                 841
                        0611
                                842
843
                        0611
                                      NEG_SIND:
50
      8000 8F
                   AA
                        0611
                                                BICW
                                                          #^x8000, R0
                                                                                         : R0/R1 = |x|
                                 844 POS_SIND:
                        0616
                                                          D 45, RO
SMALL SIND
REDUCE_DEGREES
                                845
50
      FA16 CF
                        0616
                                                CMPD
                                                                                         : Compare 45 to IXI
                   14
                        061B
                                 846
                                                BGTR
                                                                                         ; special processing for small arg
 000009CB'EF
                   16
                        061D
                                 847
                                                JSB
                                                                                         : R6/R7 = reduced argument
                        0623
                                 848
                                                                                         : R3 = octant
                                 849
                        0623
                                850 EVAL_SIND:
                        0623
                                                         R3, #0, #7
P_SIN_D-1$
P_COS_D-1$
P_COS_D-1$
P_SIN_D-1$
N_SIN_D-1$
N_COS_D-1$
N_COS_D-1$
07
      00
            53
                   8F
                        0623
                                 851
                                                CASEB
                                852
853
                068E'
                        0627
                                     15:
                                                .WORD
                ŎŠĔĬ'
                       0629
                                                .WORD
                05Ē1'
                                 854
                       062B
                                                .WORD
                068Ė '
                                 855
                        062D
                                                .WORD
                068B1
                                 856
                                                . WORD
                        062F
                062F '
                                 857
                                                . WORD
                        0631
                062F 1
                                 858
                                                . WORD
                        0633
                068B'
                                 859
                        0635
                                                . WORD
                                                          NISINID-15
                        0637
                                 860
                        0637
                                 861
                                862
863
                        0637
                                      SMALL_SIND:
                                                          D_SMALLD, RO
50
     FAO5 CF
                        0637
                                                CMPD
                                                                                           Compare 180/pi+2^-27 with ixi
                                864
865
            06
                   14
                        063C
                                                BGTR
                                                                                           No polynomial evaluation is
                   7D
31
73
13
                                                          RO, R6
P_SIN_D
RO
         50
0671
      56
                        063E
                                                MOVQ
                                                                                             necessary
                                866
867 1$:
                        0641
                                                BRW
            50
                        0644
                                                TSTD
                                                                                           Check for zero
                                868
869
870
                                                                                           Return if RO = 0
                        0646
                                                BEQL
                   71
50
      FA14
                        0648
                                                          D_SMALLEST_DEG, RO
            CF
                                                CMPD
                                                                                           Check for possible underflow on
                   15
                        064D
                                                                                              conversion to radians
                                                BLEQ
                                                                                           Underflow will occur on conversion R2/R3 = (pi/180 - 2^-6)*ix: R0/R1 = ix:*2^-6
                   31
                        064F
                                                          UNFL
          068B
                                                BRW
      F9FA CF
0300 8F
50 52
                  65
A2
60
                                                          D CONVERT, RO, R2
50
50
                        0652
                                 872
                                                MULD3
                                873
                        0658
                                                SUBW
                        065D
                                 874
                                                          R2, R0
                                                                                           RO/R1 = DSIND(|x|) = (pi/180)|x|
                                                ADDD
                   ŎŠ
                                 875 35:
                        0660
```

RSB

0699

069A

909

910

RSB

L 13

50

56

56 54

54

8000 8F

CF

CF

05

01

16

03 11

CF

Ŏ5

00

83 02 52

8F

ŎC

56 57

56 63

50 50

06F3

06F4 06F4

06F4

06F7

06FE

0700

0704

CA

**D4** 

63

62

F975

F 966

52

52

52

52

FD A242 F996 CF43

8000

2700

54

54 54

003F0000 8F

83 56

50

F 965

R6, R4 (R3), R4 961 RSB 963 NOT\_ENOUGH\_BITS: MOVQ 964 (R3), R0#^X003F0000, R0 965 BICL 966 CLRL 967 R0, (R3)+, R4SUBD3 968 RO. R6 SUBD

R6/R7 = YHI

MTHSDSING	os
-----------	----

N 13; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 Page 23 REDUCE\_MEDIUM 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1 (18) ADDD XORW RSB 54 8000 8F (R3), R4 #^X8000, R4 : R4/R5 = -YLO : R4/R5 = YLO

0707 070A 070F 0710 0710 969 970 971 972 973

```
Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 EDUCE_LARGE 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
                                                                                                                                            Page 24 (19)
                       REDUCE_LARGE
                                                      .SBTTL REDUCE_LARGE
                                      976
977
                             0710
                             0710
                             0710
                                      978
                                              This routine is used to reduce large arguments ('X' >= 9*pi/4) modulo pi/4. It returns the reduced argument, Y, in R4/R7 in units of cycles, and returns
                             0710
                                      979
                             0710
                                      980
                                              the octant bits, I, in R2.
                             0710
0710
0710
0710
                                      981
                                      982
983
                                              The method of reduction is as follows:
                                      984
985
986
987
                                                   x*(4/pi) = 2^n*f*(4/pi) where n is an integer and 1/2 = < f < 1
= 2^n(n-56)*(2^56*f)*(4/pi)
= (2^56*f)*(2^n(n-56)*4/pi)
                             0710
                             0710
                             ŎŹĬŎ
                                                               = K*C, where K = 2^56*f is an integer and C = 2*(n-56)*4/pi
                             0710
                                                   Let L = K*C modulo 8, where 0 = < L < 8, and let I = the integer(L) and h = fract(L), then if I is even Y = h, otherwise Y = 1-h
                             0710
                             0710
                             0710
                                      991
                                              CONSTANTS:
                             0710
                                      992
                                                      L_INT_WEIGHT = ^X1E80
W_TERM_WEIGHT = ^X1000
                             0710
                                      993
                 00001E80
                                                                                                  weights exponent by 61
                 00001000
                             0710
                                      994
                                                                                                  weights exponent by 32
                                                      W_MAX_WEIGHT = 1X4000
                             0710
                                      995
                 00004000
                                                                                                  maximum unbiased exponent
                                                                        = ^x39
                 00000039
                             0710
                                      996
                                                      WIADJUST
                                                                                                  Used to locate binary point in
                                      997
                             0710
                                                                                                    MTH$AL_4_OV_PI table
                             0710
                                      998 D_2_TO_32:
                                      999
     00000000 00005080
                             0710
                                                      .QUAD
                                                                ^x5080
                                                                                               : 2^32
                             0718
                                     1000
                             0718
                                     1001
                             0718
                                     1002
                                    1003 REDUCE_LARGE:
                             0718
                             0718
                                    1004
                             0718
                                              The first step is to obtain the location of the binary point in the representation of C = 2^{(n-56)*(4/pi)} in two parts - the number of longwords from
                                    1005
                             0718
                                    1006
                             0718
                                     1007
                                              the start and the number of bits from the most significant bit of the next
                             0718
                                              longword. Also K = 2^56*f must be obtained.
                                     1008
                             0718
                                     1009
                                                                #^x8000, RQ
           8000 8F
                             0718
    50
                                     1010
                                                      BICW
                                                                                                  RO/R1 = X
                        90
                                                                #-7, RO, R3
       50
             F9 8F
                             071D
                                     1011
                                                      ROTL
                                                                                                  Shift exponext field 7 bits right
                        ÀŽ
                                     1012
           53
                  39
                             0722
                                                      SUBW
                                                                WW_ADJUST, R3
                                                                                                  Unbias exp and adjust for leading
                             0725
                                                                                                    zeroes. R3 = location of binary
                             0725
                                     1014
                                                                                                    point
                                                                                                 Divide R3 by 32 and mull by 4 to get R4 = # of longwords (in bytes) to
                             0725
                                     1015
             FD 8F
                                                      ROTL
      FFFFFFE3 8F
                                                                W^XFFFFFFE3, R4
                        CA
                             072A
                                     1016
                                                      BICL
                             0731
                                     1017
                                                                                                    binary point.
52
      00000000'EF
                             0731
                                     1018
                                                                MTH$AL_4_OV_PI, R2
                        DE
                                                      MOVAL
                                                                                                  Get base address of MTHSAL_4_OV_PI
                             0738
                                     1019
                                                                                                    table
                        (2
A8
                             0738
                                     1020
                                                                R4, R2
#^XEO, R3
                                                                                                 R2 points to 1st quadword of interest R3(7:0) = # of bits within longword
             E0 8F
                             073B
                                     1021
                                                      BICB
                             073F
                                     1022
                                                                #^X7F80, RO
                             073F
                                     1023
           7F80 8F
                                                      BICW
                                                                                                 Clear exponent field RQ = 2^24*f
     50
           4000
                 8F
                             0744
                                                                #^X4C00, RO
                        8A
                                     1024
                                                      BISW
                                                                RO, RO
#16, R1, R1
                                                                                                 RO = High 24 bits of K
R1 = Low 32 bits of K
                             0749
           50
                  50
                        6A
                                     1025
                                                      CVTDL
           51
                        90
     51
                  10
                             0740
                                     1026
                                                      ROTL
                  02
50
                        18
                             0750
                                     1027
                                                      BGEQ
                                                                15
                                                                                                 Check for high bit of R1 set
                             0752
                                                                RO
                        D6
                                     1028
                                                      INCL
                                                                                                 Adjust RO if R1 is negative
                             0754
                                     1029
                                     1030
                                     1031
                                           ; The next step is to generate an approximation to C, call it C'' to be used
```

B 14

MTH\$DSINCOS 2-007	; Floating Point Sine, REDUCE_LARGE	D 14 Cosine and Sincos 16-SEP-1984 01:2 6-SEP-1984 11:2	20:38 VAX/VMS Macro VO4-00 Page 26 22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1 (19)
57 54 0C 67 62 53 57 04 52 04 67 62 53	076A 1089; 076A 1090 C1 076A 1091 076E 1092 79 076E 1093 0772 1094 C2 0772 1095 C2 0775 1096 2\$: 0778 1097 79 0778 1098 077C 1099	ASHQ R3, (R2), (R7)  SUBL #4, R7  SUBL #4, R2  ASHQ R3, (R2), (R7)	Initailize loop counter. R7 points to T7 Shift the proper quadword so that T8 has C(0) in it R7 points to T6 R2 points to next quadword in MTH\$AL 4_OV_PI table Shift quadword so that C(n) is in T(8-n) n= 0.1.2.3
FFEA 57 FFFFFFFC 8F 54	18 077C 1100 D6 077E 1101 F1 0781 1102 3\$: 078B 1103 078B 1104 078B 1105; 078B 1106; Gener	BGEQ 3\$ INCL 8(R7) ACBL R4, #-4, R7, 2\$  ate the low 128 bits of the produc	; theck for high bit of t(n) set; ; Bit set. Adjust C(n-1); ; Loop until C(0) though C(3) are in; ; To though T8
	078B 1107 ; equiv 078B 1108 ; produ 078B 1109 ; 125 b 078B 1110 ; 20:0	alent to multiplying K times (''') ict is in T4/T7 with bits 31:29 of its the faction bits of the product of T6 and 31:0 of T5) are non-valued if more fraction bits need to be	modulo 8. The result of the T4 the octant bits, and the remaining ct. The last 53 fraction bits (bits id fraction bits that will be used
04 AE 04 AE 08 A4 50 04 AE 04 AE 08 A4 50 64 0C A4 50 08 AE 64	078B 1114; Multi 078B 1115; T0/T2 078B 1116 7A 078B 1117 7A 0791 1118 C5 0799 1119 C0 079E 1120	EMUL RO, 4(R4), #0, (SP) EMUL RO, 8(R4), 4(SP), 4(SP)	times C'' and store the result in : T0/T1 = KHI*C(3) : T0/T2 = KHI*C(2):C(3)] : T4 = Low 32 bits of KHI*C(1) : T0/T2 = KHI*C'' modulo 8
64 00 04 A4 51 04 A4 04 A4 08 A4 51	07A2 1121 07A2 1122 : Multij 07A2 1123 : T4/T8 07A2 1124 7A 07A2 1125	ply the low order bits of K (R1) to .  FMUL R1 4(R4) #0 (R4)	
0C A4 65 04 A4 6E	C4 07B8 1128 C0 07BB 1129 07BF 1130 07BF 1131; Add KI 07BF 1132 C0 07BF 1133	HI*C'' to KLO*C'' to get K*C''. S ADDL (SP), 4(R4)	; 14/1/ = KLU*C = moduto 8
08 A4 04 AE 0C A4 08 AE	07CD 1139; Y. I 07CD 1140; loss; 07CD 1141; of si	ADWC 4(SP), 8(R4) ADWC 8(SP), 12(R4)  is point there may or may not be of the first 12 fratction bits are of significance when computing Y. gnificance before converting 14/Ti	enough valid bits in R3/R4 to generate all 1's or 0's, there a possibility of Consequently, we must check for loss 7 to Y and I.
65 FC A5 00200000 8F 65 3FC00000 8F	07CD 1142; 07CD 1143 C1 07CD 1144 D3 07D6 1145	ADDL3 #^X200000, -4(R5), (R5) BITL #^X3FC00000, (R5)	; If the first 12 fraction bits are 1's ; and the reduced arg = 1-f or the

```
07DD
07DF
                     37
                                      1146
                          12
                                                      BNEQ
                                                               CONVERT
                                                                                                first 7 bit are 0 and the reduced
                                                                                                arg = f, then (and only then) bits
29:22 are 0 and significance will
                                07DF
                                      1148
                                07DF
                                       1149
                                                                                                be lost.
                                07DF
                                       1150
                                07DF
                                       1151
                                      1152
1153
                                               More bits need to be generated to cover the loss of significance. There are not enough registers to hold all the potential entra bits, so that the bits
                                07DF
                                07DF
                                      1154
                                07DF
                                               already generated must be put on the stack.
                                07DF
                                07DF
                                       1156
                               07DF
07E5
          0000090B'EF
                                       1157
                           16
                                                      JSB
                                                               GEN_MORE_BITS
                                                                                              Generate 85 additional bits and add
                                                                                                them to existing bits. Results are
                                       1158
                                07E5
                                       1159
                                                                                                stored in 13/17
                                07E5
               54
                     04
                           C2
                                      1160
                                                      SUBL
                                                               #4, R4
                                                                                              Adjust R4 to reflect the addition of
                               07E8
07E8
                                                                                                another longword of K+C'
                                       1161
        15 FC A5
                     1 D
                           E0
                                      1162
                                                                                              Check if loss of significance is due
                                                      BBS
                                                               #29, -4(R5), 4$
                                07ED
                                      1163
                                                                                                to leading ones or zeros
                                07ED
                                      1164
                                07ED
                                      1165; Lost significance due to leading zeros
                                07ED
                                      1166
                               07ED
07F3
65
      10 A4
               15
                                      1167
                                                               #0, #21, 16(R4), (R5)
                                                                                            : If at least one bit is set. This
                                       1168
                                                      BNEQ
                                                               CONVERT
                                                                                                means lost significance was minor.
                               07F5
07FD
07FF
                     8F
                                                               #AX1FFFFFFF, 12(R4)
 OC 44
          1FFFFFFF
                           D1
                                      1169
                                                      CMPL
                                                                                              If one of the three high bits is set,
                           15
31
                                       1170
                                                      BLEQ
                                                               CONVERT
                                                                                                lost significance was minor.
                   00B2
                                       1171
                                                      BRW
                                                               LEADING_ZEROS
                               0802
0802
0802
0802
0808
0808
0812
0814
0816
                                       1172
                                       1173
                                            ; Lost significance due to leading ones
                                       1174
                                      1175 48:
65
      10 A4
               15
                                                      FFC
                                                               #0, #21, 16(R4), (R5)
                                                                                            ; If at least one bit is clear. This
                                      1176
                                                      BNEQ
                                                               CONVERT
                                                                                                means lost significance was minor.
          E0000000
 OC A4
                     8F
                           D1
                                      1177
                                                      CMPL
                                                               #^XE0000000 12(R4)
                                                                                              If one of the three high bits is
                           1E
                                      1178
                                                      BGEQU
                                                               CONVERT
                                                                                              clear, lost significance was minor.
                                      1179
                                                      BRB
                                                               LEADING_ONES
                                      1180
                                0816
                                      1181
                                0816
                                      1182 CONVERT:
                                0816
                                      1183
                                C816
                                      1184
                                                  Isolate octant bits and convert fraction bits to a pair of D-format
                               0816
0816
0816
                                      1185 :
                                                  quantities YHI and YLO
                                      1186
65 FC A5
                                                               #29. #3. -4(R5). (R5)
               03
                                      1187
                                                      EXTZV
                                                                                             T8 = octant bits
                                0810
 FC A5
                           CA
C3
          E0000000 8F
                                      1188
                                                      BICL
                                                               #^XEO000000, -4(R5)
                                                                                              Clear octant bits
                               0824
0828
                                                                                             R4 points to low order bits of h
R0/R1 = 2^29*h_lo
R6/r7 = 2^29*h_hi
                     ОC
                                                               #12, R5, R4
                                      1189
                                                      SUBL 3
          00000951'EF
                                      1190
                                                               CVT_TO_DOUBLE
                                                      JSB
                                082E
                                       1191
                               082E
0833
               0E80 8F
                                      1192
                                                               #^XE80, R6
                                                                                              R6/R7 = h_hi
         56
                     Õ2
                                      1193
                                                      BGTR
                                                               3$
                                                                                              Check for h_hi = 0
                     56
                                0835
                           D4
                                                      CLRL
                                       1194
                                                               R6
                                                                                              Restore h_hi to 0
                           B5
13
                     50
                                0837
                                      1195 35:
                                                      TSTW
                                                               RÔ
                                                                                             theck for h_lo = 0
                     05
                                0839
                                      1196
                                                      BEQL
                           AZ
E9
                                                               #*XE80, RO
(R5), 2$
         50
                                083B
               0E80
                     8F
                                       1197
                                                      SUBW
                                                                                              RO/RI = h_lo
                  07
                     65
                                0840
                                       1198 15:
                                                      BLBC
                                                                                            ; Check for odd or even octant bits
                                0843
                                       1199
                                0843
                                       1200
                                                  Octant bits are odd. Reduced argument equals 1 - h.
                                0843
                                       1201
                                0843
         56
                     56
                           63
                                       1202
               08
                                                      SUBD3
                                                               R6. #1. R6
                                                                                           : R6/R7 = Y = 1 - h_hi
```

#29, #3, 8(SP), R2

RESTORE

correct choice is determined by the calling program based on the octant bits

; Reduced argument is zero

: R2 = octant bits

1254

1255

1256 1257 returned in R1.

EXTZV

BRW

0885

0885

0885 0885

0887

0880

52

08 AE

Si

```
Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 EDUCE_LARGE 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
                              REDUCE_LARGE
                                     0890
                                                    CONVERT_1:
                                      0890
                                                                                                              R4 points to low bits of h

R0/R1 = 2^W*h_lo

R6/R7 = 2^W*h_hi

R6/R7 = 2^W*(T - h_hi)
                                                                           #4, R4
CVT_TO_DOUBLE
            00000951'EF
                                16
                                     0893
                                                                JSB
                                     0899
                                                                          R6, D_2_T0_32, R6
R0, R0
#29, #3, -4(R5), R2
                               63
72
F C2
B5
13
C2
11
                                     0899
    56
          FE72 CF
                                                                SUBD3
                         56
50
10
65
50
                  50
03
56
                                     089F
                                                                MNEGD
                                                                                                               RO/R1 = -2*W+h Lo
52
      FC A5
                                     SA80
                                                                EXTZV
                                                                                                               R2 = octant bits
                                     08A8
                                                                SUBL
                                                                           (R5), R6
                                                                                                               R6/R7 = 1 - h hi
                                                                TSTW
                                     08AB
                                                                           RO
                                                                                                               Check for h_l\bar{o} = 0
                         4A
65
45
                                                                           GET YHI YLO
                                     08AD
                                                                BEQL
                  50
                                     08AF
                                                                SUBL
                                                                                                              RO/R1 = - h_lo
                                     0882
                                                                BRB
                                                                           GET_YHI_YLO
                                      08B4
                                             0884
                                     0884
                                                      If processing continues here it is known that the loss of significance is due to a string of leading zeros. Note that it is known that the loop for
                                     08B4
                                     08B4
                                                       leading zeros will terminate before an underflow condition occurs so that the
                                     08B4
                                                    ; loop does not include a test for underflow.
                                     08B4
                                     0884
0888
            00001E80 8F
                                                                           #L_INT_WEIGHT, (R5)
                                                                                                            ; T8 = exp bias for last longword
                                                                                                                   of the product K*C'
                                     08BB
                                                                          #^X001FFFFF, 12(R4)
CONVERT_0
GEN_MORE_BITS
12(R4)
CONVERT_0
4(R4), 8(R4)
-4(R4), (R4)
#W_TERM_WEIGHT, (R5)
LOOP_0
                                     08BB
08C5
08CB
08CE
08DC
 OC A4
            001FFFFF 8F
                                                                                                               Check enough fraction bits
                                19
                                                                                                               Enough bits. Convert to floating
                                                                                                              T2/R7 contain K*C''
Check for all 0's
Not all 0's. Enough precision bits.
            0000090B'EF
                                16
                                D5
12
                    OC A4
                         10
                                7D
                                                                                                               Compress representation of K*C'
         08 A4
                                7D
                                     08D5
                         A4
             64
                 1000 8F
                                AO
          65
                                     08D9
                                                                                                             ; Increment weighting factor.
                                11
                                     08DE
                                     08E0
                                             1296
1297
1298
1299
                                                    CONVERT_0:
                                     08E0
                                                                                                              R4 points to low bits of h
R0/R1 = 2^W*h_lo
R6/R7 = 2^W*h_hi
                                     08E0
                                                                ADDL
                                                                          #4, R4
CVT_TO_DOUBLE
            00000951 EF
                                     08E3
                                16
                                                                JSB
                                     08E9
                               EF
C2
B5
13
C2
                        1D
65
                                     08E9
                                              1300
                                                                           #29, #3, -4(R5), R2
(R5), R6
52
                                                                EXTZV
    FC A5
                                                                                                               R2 = octant bits
                                                                                                              R6/R7 = h_hi
                                              1301
                  56
                                     08EF
                                                                SUBL
                         50
                                     08F2
                                              1302
                                                                TSTW
                                                                           RO
                                                                                                               Check for h_lo = 0
                                             1303
1304
                                                                          GET YHI YLO
                         03
                                     08F4
                                                                BEQL
                  50
                                     08F6
                                                                                                               R0/R1 = h_lo
                                                                SUBL
                                              1305
                                     08F9
                                             1306 GET_YHI_YLO:
1307 MOVQ
1308 CLRL
1309 SUBD
                                     08F9
                         56
57
                                     08F9
                                                                                                               R4/R5 = high bits of Y
                  54
                                                                           R6, R4
                                04
                                     037.0
                                                                           R7
                                                                                                               R6/R7 = high 24 bits Y = YHI
                         56
50
                  54
54
                                62
                                     08FE
                                                                           R6, R4
                                60
                                     0901
                                              1310
                                                                ADDD
                                                                           RO. R4
                                                                                                              R4/R5 = YLO
                                     0904
                                              1311
                                                    RESTORE:
                 5E<sup>24</sup>
                                             1312
1313
1314
                                B8
(0
05
                        AE
28
                                     0904
                                                                BISPSW
                                                                           36(SP)
                                                                                                              Restore IV bit and exit
                                     0907
                                                                           #40, SP
                                                                ADDL
                                                                                                            ; Pemove mask and temporary storage
                                     090A
                                                                RSB
```

090B

090B

1315

1316

G 14

PS ---

Sy

Ph In Cay Sya Sya Cr

Cr As Th 38

18

10

Ma

```
Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
                              REDUCE LARGE
                                          1317 GEN_MORE_BITS:
                                     090B
                                     090B
                                           1319
                                                    This subroutine generates 85 extra fraction bits and puts them to the existing bits. NOTE: This routine is always entered via a JSB instruction.
                                     090B
                                     090B
                                     090B
                                                    Consequently, SP points to the first longword BEFORE TO, rather than TO
                                     090B
                                                    itself.
                                     090B
                                     090B
                   52
                                    090B
                         04
                               C 2
                                                            SUBL
                                                                      #4, R2
                                                                                                   : Adjust pointer to get next quadword : _from MTH$AL_4_OV_PI
                                     090E
                         53
17
                               79
18
                                    090E
             56
                   62
                                                                                                     R7 = C(n)
                                                            ASHQ
                                                                      R3, (R2), R6
                                     0912
                                                            BGEQ
                                                                                                   ; Branch if high bit is clear
                                     0914
                                     0914
                                            1331 ; Logic to process unsigned values greater than 2^31 - 1
                                     0914
                                    0914
091A
091E
0925
                         51
51
50
                                            1333
                                                                     R1, R7, #0, 4(SP)
R1, 8(SP)
R0, R7, 8(SP), 8(SP)
R0, 12(SP)
   04 AE
             00
                                                            EMUL
                08 AE
                                00
                                            1334
                                                            ADDL
                                                                                                     TO/T1 = KLO*C(n)
                                ŽĂ.
         08 AE
                                            1335
08 AE
                   57
                                                            EMUL
                         50
                               CO
                OC AE
                                            1336
                                                            ADDL
                                                                                                   : T0/T2 = K*C(n)
                                    0929
                          Q0
                               11
                                            1337
                                                            BRB
                                     092B
                                            1338
                                     092B
                                            1339; Logic to process unsigned values less than 2^31
                                     092B
                                            1340
                   57
57
                                    092B
                                            1341 15:
                                                                     R1, R7, #0, 4(SP)
R0, R7, 8(SP), 8(SP)
   04 AE
                                                            EMUL
                                                                                                   ; TO/T1 = KLO*C(n)
08 AE
         08 AE
                         50
                               7A
                                    0931
                                           1342
                                                                                                   : T0/T2 = K*C(n)
                                                            EMUL
                                     0938
                                            1343
                                           1344; Add new bits to old
1345
1346 2$: ADDL 8(SP)
1347 ADWC 12(SP)
1348 BCC 3$
                                     0938
                                     0938
                                                                     8(SP), (R4)
12(SP), 4(R4)
                      08 AE
                                    0938
                               CO
            04 A4
                      OC AE
                               D8
                                    093C
                               1E
                                    0941
                         80
                                                                                                     Check for carry from previous add
                     80
                                            1349
                                    0943
                                                            INCL
                                                                      8(R4)
                         A4
                               D6
                                                                                                     Propagate carry
                                1E
                                    0946
                                            1350
                         03
                                                                      3$
                                                            BCC
                                                                                                     Check for carry from previous add
                                            1351
                                                                      12(R4)
                      OC A4
                               D6
                                    0948
                                                            INCL
                                                                                                     Propagate carry
                     04
                               DÕ
                                            1352 35:
            FC A4
                         ΑE
                                    094B
                                                                      4(SP), -4(R4)
                                                            MOVL
                                                                                                     Move new low order bits to end of
                                     0950
                                            1353
                                                                                                        of old low order bits
                                            1354
                               05
                                    0950
                                                            RSB
                                     0951
                                            1355
                                            1356
                                     0951
                                            1357
                                            1358
                                           1360 CVT_TO_DOUBLE:
                                                    This routine converts an array of three longword pointed to by R4 to a pair
                                            1364
                                                    of D-format values. The results are returned in RO/R1 (low 48 bits) and
                                     0951
                                            1365
                                                    R6/R7 (high 48 bits).;
                                            1366
                                     0951
                   50
                                    0951
                                            1367
                               6E
13
                                                            CVTLD
                                                                      (R4)+, R0
                                                                                                     R0/R1 = Low 32 bits of h
                          OE
                                    0954
                                            1368
                                                            BEQL
                                                                      28
                                            1369
1370
                         07
                               14
                                    0956
                                                            BGTR
                                                                      15
                                                                                                     Adjust for signed
                                    0958
                                                            INCL
                                                                      (R4)
                          64
                               D6
                                                                                                        conversion error
                          03
                                    095A
                                            1371
                                1E
                                                            BCC
                                                                      18
                                                                                                     If necessary,
                                    095C
                                            1372
                                                                      4(R4)
                                                            INCL
                         A4
                                D6
                                                                                                   propagate carry
RO/R1 = (low 32 bits of h)/2*32
                                            1373 15:
             50
                   1000
                                A2
                                     095F
                         8F
                                                            SUBW
                                                                      #W_TERM_WEIGHT, RO
```

H 14

FC A4 64

	; Flo REDUC	ating E_LAR	Point GE	Sine,	Cosine	I 14 and Sincos	16-SEP-19 6-SEP-19	84 01:20:38 84 11:22:35	VAX/VMS Macro VO4-00 [MTHRTL.SRC]MTHDSINCO.MAR;1	Page	31 (19)	
3F	(B	0964 0960	1374 1375	2\$:	BICL3	#^XFFFF00 -4(R4), (	000, (R4),	-4(R4)				

50 FFF	F0000 8F FC A4 FC A4 50 52 05 1000 8F 52 84	02E032E3	0964 096D 0971 0975 0978 097A 097F 0982	1374 2\$: 1375 1376 1377 1378 1379 1380 3\$: 1381	BICL3 SUBL CVTLD ADDD BEQL SUBW CVTLD BEQL	#^xffff0000, (R4), -4(R4) -4(R4), (R4) -4(R4), R2 R2, R0 3\$ #W_TERM_WEIGHT, R0 (R4)+, R2 5\$	RO/R1 = (low 48 bits of h)/2^32 RO/R1 = (low 48 bits of h)/2^64 R2/R3 = next 16 bits of h
52 56	02 64 1000 8F 56 64 05 FD7A CF 56 52	14 DA2 6E 18 605 05	0984 0988 0988 0980 0992 0997 0998	1382 1383 1384 4\$: 1385 5\$: 1386 1387 1388 6\$: 1389 1390	BGTR INCL SUBW CVTLD BGEQ ADDD ADDD RSB	4\$ (R4) #W_TERM_WEIGHT, R2 (R4), R6 6\$ D_2_TO_32, R6	Adjust for signed conversion error. Note that no carry is possible R2/R3 = (next 16 bits of h)/2*32 R6/R7 = high 32 bits of h Adjust for signed conversion error R6/R7 = (high 48 bits of h)/2*32

```
floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 (EDUCE_DEGREES 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
                           REDUCE_DEGREES
                                   099B 1392
099B 1393
                                                                .SBTTL REDUCE_DEGREES
                                   0998
                                                      This routine assumes that the absolute value of the argument is in RO/R1.
                                           1395: The reduction process is performed in two stages. The first stage of 1396: the reduction reduces the argument modulo 360 to a value less that 2^55, 1397; and the second stage reduces the argument modulo 45 to a value less than 45.
                                   099B
                                   099B
                                            1398
                                   099B
                                           1399
                                   099B
                                                   : Constants used in this reduction:
                                           1400 :
                                   099B
                                   099B
                                            1401
                                           1402 POWER_MOD_360_0:
1403 .WORD
                                   099B
                                                                                        ; Powers of 2 modulo 360 for t1 = 0
  0008 0004 0002 0001
0080 0040 0020 0010
                                                                                       32.
152.
                                   099B
                                                                           16,
                                                                                                                128
248
                                   09A3
                                            1404
                                                                .WORD
   00f8 0130 0098 0100
                                   09AB
                                                                                                    3Õ4.
                                            1405
                                                                           256.
                                                                . WORD
                                   09B3
                                            1406
                                           1407 POWER_MOD_360_1:
                                   09B3
                                                                                          Powers of 2 modulo 360 for t1 <> 0
                                                                                       272,
32,
152,
                                                                          136,
   0008 00B8 0110 0088
                                   09B3
   0080 0040 0020 0010
                                                                           16.
                                   09BB
                                            1409
                                                                                                    64.
304.
                                                               . WORD
   00F8 0130 0098 0100
                                   0963
                                                                           256.
                                            1410
                                                                . WORD
                                   09CB
                                           1411
                                   09CB 1412
                                   09CB 1413
                                   09CB 1414 REDUCE_DEGREES:
      50
             5000 8F
                                                               CMPW
                                   09CB
                                           1415
                                                                           #^x5c00, RO
                                                                                                                : Compare 1x1 with 2^55
                     49
                            14
                                  09D0
                                           1416
                                                               BGTR
                                                                            LAST_STEP
                                                                                                                ; Branch to special logic for med arg
                                   0902
                                           1417
                                   0902
                                           1418
                                   09D2 1419
                                                   ; It is assumed here that the argument is greater than 2^55.
                                           1420
                                   09D2
                                                      The argument is reduced as follows:
                                                            Let x = 2^{\circ}t*f, where t > 56 and 1/2 = < f < 1. And let J = 2^{\circ}56*f = 2^{\circ}30*J1 + J2 and K = 2^{\circ}(t-56). Since 2^{\circ}30 = 64 modulo 360, we have that J = 64*J1 + J2 modulo 360. Now let t' = t - 56 = 12*t1 + t2. Note that (2^{\circ}12)^{\circ}2 = (2^{\circ}9)*(2^{\circ}15) = (2^{\circ}9)*(2^{\circ}3) = 2^{\circ}12 modulo 360. Hence, if t1 is
                                   09D2
                                   09D2
                                   09D2
                                   09D2
                                                            not zero, K = 2^{\circ}t' = 2^{\circ}(12*t1+t2) = (2^{\circ}12)*(2^{\circ}t2) = 136*2^{\circ}t2 modulo 360. For t1 = 0 K = 2^{\circ}t2. Consequently, define K' congruent to 2^{\circ}t2 if t1 = 0 and congruent to 136*2^{\circ}t2 otherwise, where 0 =< K' < 360. Then x' = K'*(64*J1 + J2) is congruent to s modulo 360 and x' < 2^{\circ}56.
                                   09D2
                                           1426
                                   09D2
                                           1427
                                   09D2
                                           1428
                                           1429
                                   0902
                                   0902
                                           1430
       52 50
00007F80 8F
                                  0902
                            D0
                                           1431
                                                               MOVL
                                                                                                                ; R2 = high longword of X
                                                                           #^x7F80, RO
50
                                   09D5
                                                                                                                ; Clear exp bits of X
                            CA
                                           1432
                                                               BICL
                                                                                                                : RO/R1 = J
      50
             5000 8F
                             88
                                   09DC
                                           1433
                                                               BISW
                                                                           #^x5c00, R0
                            CŽ
             52
                     50
                                  09E1
                                            1434
                                                               SUBL
                                                                           RO. R2
                                                                                                                : R2 = t' * 2^7
                                   09E4
                                           1435
       53 50
FFFF3FFF 8F
                            70
                                  09E4
                                           1436
                                                               MOVQ
                                                                                                                : R3/R4 = J
                             CA
                                   09E7
                                            1437
                                                               BICL
                                                                           #^XFFFF3FFF, R1
                                                                                                                  RO/R1 = J1*2^30
                                                                                                                 R3/R4 = J2
                     50
                            62
                                   09EE
                                            1438
             53
                                                               SUBD
                                                                           RO, R3
             0000 8F
      50
                             A2
                                   09F1
                                            1439
                                                                           #^XC00, R0
                                                               SUBW
                                                                                                                 R0/R1 = 64*J1
                     53
                            60
                                   09F6
                                                                           R3, R0
                                                                                                                : R0/R1 = 64*J1 + J2 = J modulo 45
                                            1440
                                                               ADDD
                                   09F9
                                            1441
             F9 8F
52 0C
53 0C
52 53
                                                                                                               ; R2 = t'
; R3 = t1
; R3 = 12*t1
                                                                           M-7, R2, R2
M12, R2, R3
M12, R3
 52 52
                                   09F9
                                            1442
                                                               ROTL
                            ÀŽ
                                            1443
                     00
                                   09FE
                                                               DIVW3
                                   0A02
                                            1444
                                                               MULW
                             44
                     53
                             A2
                                   0A05
                                            1445
                                                               SUBW
                                                                           R3, R2
                                                                                                                : R2 = t2
                                   80A0
                                            1446
                     53
07
                                                                                                               ; Check for t1 = 0 and choose K'
                                   80A0
                                            1447
                                                               TSTW
                             12
                                   0A0A
                                            1448
                                                               BNEQ
                                                                                                               ; accordingly
```

J 14

```
Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00
6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO
MTH$DSINCOS
2-007
                                      REDUCE_DEGREES
                                                                                                                   [MTHRTL.SRC]MTHDSINCO.MAR:1
                                                    1449
1450
1451
1453
1453
1455
1457
                     52
                           8B AF42
05
                                       6D
                                                                    CVTWD
                                                                              POWER_MOD_360_0[R2], R2 ; R2/R3 = K'
                                             0A11
                                                                    BRB
                     52
                                             ŎA13
                                                                    CVTWD
                                                                             POWER_MOD_360_1[R2], R2; R2/R3 = K'
R2, R0 ; R0/R1 = X'
                                        6D
                                                         15:
                                             0A18
                                        64
                                                          25:
                                                                    MULD
                                                                                                            R\bar{O}/R1 = X' \pmod{45} \ 0 = < RO < 2^5
                                             OA1B
                                             OA1B
                                             OA1B
                                                          LAST_STEP:
                                             OA1B
                                             OA1B
                                                            Argument reduction scheme for arguments with absolute value less than 2^55
                                             0A1B
                                                    1459
                                             OA1B
                                                            The reduced argument Y is computed as follows:
                                             OA1B
                                                                Let I = int(X/45)
if I is even
                                                    1460
                                             0A1B
                                                    1461
                                                    1462
                                             0A1B
                                                                       then Y = X - 45*I
                                                                       else Y = (I+1)*45 - x
                                                    1463
                                             OA1B
                                                    1464
                                             0A1B
                                                    1465
                                                                             #^X5200, RO
NO_OVERFLOW
                     50
                           5200 BF
                                             0A1B
                                                                    CMPW
                                                    1466
                                                                                                           : Compare 2^36 with IX!
                                       18
                                             0A20
                                                                    BGEQ
                                                    1467
               56
                     50
                           F622 CF
                                             0A22
                                                    1468
                                                                                                           : R6/R7 = |x|/45
                                                                    MULD3
                                                                             D_T_OV_45, RO, R6
                                             OA28
                                                    1469
                                                    1470
                                                    1471
                                             0A28
                                                            Turn off IV to avoid an exception in EMODD
                                                    1472
                                             0A28
                                            0A28
                                                                    MOVPSL
                                                                                                             Move PSL to R2
Save current IV bit
                                       CA
B9
                52
                      FFFFFFDF 8F
                                                                              W^C<PSL$M_IV>, R2
                                             0A2A
                                                    1474
                                                                    BICL
                                             0A31
                                                    1475
                                                                             #PSL$M_IV
                                  20
                                                                    BICPSW
                                                                                                           : Turn off integer overflow trap
                                             0A33
                                                    1476
         54
               53
                           00
                                        74
                                                    1477
                     56
                                 80
                                                                    EMODD
                                                                                                          ; R3 = low 32 integer bits of \times \text{1X1/45}
; R4/R5 = fractional part of \text{1X1/45}
                                                                             #1, #0, R6, R3, R4
                                             0A39
                                                    1478
                                                    1479
                                             0A39
                                 52
                                       B8
                                            0A39
                                                    1480
                                                                    BISPSW
                                                                                                           : Restore IV bit
                                             0A3B
                                                    1481
                                 54
53
                           56
                                       62
E9
                                            0A3B
                                                                    SUBD2
                                                                             R4, R6
R3, EVEN
                                                                                                             R6/R7 = Integer part of |X|/45 = I
                              27
                                            0A3E
                                                    1483
                                                                    BLBC
                           56
                                 80
                                       60
                                                                             #1. R6
                                            0A41
                                                    1484
                                                                    ADDD2
                                                                                                           : R6/R7 = I + 1
                                  12
                                        11
                                            0A44
                                                    1485
                                                                    BRB
                                                                             ODD
                                            0A46
                                                    1486
                                            0A46
                                                    1487
                                            0A46
                                                    1488 NO_OVERFLOW:
   54
         53
               50
                     08
                           F5FE CF
                                        74
                                            0A46
                                                    1489
                                                                    EMODD
                                                                             D_1_OV_45, #X_1_OV_45, RO, R3, R4
                                                                                                             R3 = 1 = integer part of 1X1/45
                                            OA4E
                                                    1490
                                       E9
                                            OA4E
                                                    1491
                                                                                                             Branch if octant bits are even
                              14
                                                                    BLBC
                           53
                                 01
56
                                        C1
                                            0A51
                                                    1492
                                                                    ADDL3
                                                                             #1, R3, R6
                     56
                                                                                                             R6 = I + 1
                                                    1493
                                                                             R6, R6
D 45, R6
R0, R6
                                            0A55
                                                                                                             R6/R7 = I + 1
                           56
                                       6E
                                                                    CVTLD
                             5D4 CF
6 50
F8 8F
                                       64
                                                    1494 ODD:
                     56
                           F 5 D 4
                                            0A58
                                                                    MULD2
                                                                                                             R6/R7 = 45*(I+1)
                           56
                                            OA5D
                                                    1495
                                                                    SUBD2
                                                                                                             R6/R7 = Y
                        53
                                       8A
05
                                                                             #*XF8, R3
                                            0A60
                                                    1496
                                                                    BICB
                                                                                                           : Save only last three octant bits
                                            0A64
                                                    1497
                                                                    RSB
                                             0A65
                                                    1498
                                                                             R3, R6
D M45, R6
R0, R6
                                            0A65
                                       6E
                                                    1499 CVT:
                                                                    CVTLD
                                                                                                             R6/R7 = 1
                           FSCC CF
                                                    1500 EVEN:
                                       64
                                            0A68
                     56
                                                                    MULDS
                                                                                                             R6/R7 = -45*1
                                            OA6D
                                  50
                                                    1501
                            56
                                                                    ADDD2
                                                                                                             R6/R7 = Y
                                                    1502
1503
1504
1505
                        53
                             F8 8F
                                       8A
05
                                            0A70
                                                                             #^XF8, R3
                                                                    BICB
                                                                                                          ; Save only last three octant bits
                                            0A74
                                                                    RSB
                                             0A75
```

**0A75** 

K 14

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; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 Page 34 REDUCE_DEGREES 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1 (22)
                                                               0A75 1507
0A75 1508
0A75 1509
                                                                                                                 .SBTTL RADIAN_POLYNOMIALS ; Polynomials for arguments in radians
                                                                0A75
                                                                            1510
                                                                0A75
                                                                               1511
                                                                0A75 1512;
0A75 1513; Polynomial evaluation for DCOS(Y) for Y in radians
                                                               0A75 1515
0A75 1516 P_COS_R:
0A75 1517 E
0A78 1518
                                                                                                             BICW3
53
                          8000 8F
                                                                                                                                       #^X8000, R6, R3
                                                                                                                                                                                                       Compare 1/2 with :YHI:
                           4000 8F
                                                                                                                                       #^X4000, R3
                                                                                                                  CMPW
                                        31
                                                               0880
                                                                            1519
                                                                                                                 BGTR
                                                                                                                                       LEQL_HALF
                                                                                                                                                                                                       : Sufficent overhang is available
                                                                              1520 NEEDS_DOUBLE:
                                                                0A82
                                                                                                                                      R4, -(SP) ; Save YLO ; Save YLO ; Save YLO ; Save Y ; R0/R1 = Y^2 ; R0/R1 = Q(Y^2) ; R0/R1 = Q(Y^2) ; R4/R5 = Y + YH ; R4/R5 = Y + 
                                       54
56
6E
50
8E
                                                               0A82 1521
                                                                                                                  MOVQ
                                                                                                                 ADDD3
MULD3
POLYD
ADDD3
MULD
BEQL
SUBW
SUBW
SUBW
                                                               0A85
                                                                               1522
                                                     61
                                                    65
75
61
                          6<u>E</u>
                                                               0A89 1523
F675 CF
                                                               0A8D 1524
                                                               0A93 1525
                           56
                                                                                                                                                                                                           R4/R5 = Y + YHI
                                       8E
05
                                                               0A97
                                                                              1526
                                                    643
A2264
A2265
O5
                                                                                                                                       (SP)+, R4
                                                                                                                                                                                                           R4/R5 = YL0*(Y + YHI) = A2
                                                                                                                                                                                                      Check for A2 = 0

R4/R5 = A2/2

R0/R1 = G(Y^2) - A2/2

R6/R7 = YHI^2
                                                               0A9A
                                                                              1527
                                                                                                                                       # X80, R4
R4, R0
                          0800
                                       8F
                                                               0A9C
                                                                              1528
                          50 54
56 56
0080 8F
                                                               OAA1
                                                                               1529 18:
                                                               OAA4
                                                                            1530
                                                                                                                                       R6. R6
                                                                                                                                                                                                       ; R6/R7 = YHI^2/2
; R6/R7 = -(1 - YHI^2/2)
                                                                                                                                       #^X80, R6
             56
                                                               OAA7
                                                                               1531
                                                                                                                  SUBW
                           56
50
                                        08
                                                                               1532
                                                               DAAC
                                                                                                                  SUBD
                                                                                                                                      #1, R6
                                                                                                                                       R6. R0
                                                               OAAF
                                                                               1533
                                                                                                                  SUBD
                                                                                                                                                                                                       : RO/R1 = DCOS(Y)
                                                               0AB2
                                                                               1534
                                                               OAB3
                                                                               1535
                                                                              1536 LEQL_HALF:
                                                                OAB3
                                                                                                                                      R4, R6
                                                     60
                                                               0AB3 1537
                                                                                                                 ADDD
                          56
                                                                                                                                                                                                       : R6/R7 = Y
                                                    64
75
05
                         56
07
                                        56
                                                               0AB6
                                                                               1538
                                                                                                                                                                                                       : R6/R7 = Y^2
                                                                                                                 MULD
F609 CF
                                                               OAB9
                                                                               1539
                                                                                                                 POLYD
                                                                                                                                       R6, #COSLENR1-1, COSTBR1; RO/R1 = DCOS(Y)
                                                               OABF
                                                                               1540
                                                               OACO
                                                                               1541
                                                               OACO
                                                                               1542
                                                               OACO
                                                               OACO 1544; Polynomial evaluation for -DCOS(Y)
                                                               OACO 1545 :
                                                               OACO
                                                                               1546
                                                             OACO 1546
OACO 1547 N_COS_R:
OACO 1548 B
OAC6 1549 C
OACB 1550 B
OACD 1551 M
OADO 1552 A
OAD4 1553 M
OADE 1555 A
OADE 1556 M
OAE2 1556
                          8000 8F
                                                                                                                 BICW3
                                                                                                                                      #^X8000, R6, R3
53
                                                                                                                                      #^X4000, R3
                                                                                                                                                                                                       ; Compare 1/2 with !YHI!
                          4000
                                       8F
                                                    B1
                                                                                                                  CMPW
                                                                                                                                      2$
R4, -(SP)
R6, R4, -(SP)
(SP), (SP), R0
                                                     14
                                       32
54
56
650
8E
                                                                                                                  BGTR
                                                                                                                                                                                                       : Sufficent overhang is available
                         7E 5E 076 54
                                                     7D
                                                                                                                 MOVQ
                                                                                                                                                                                                       : Save YLO
                                                    61
                                                                                                                  ADDD3
                                                                                                                                                                                                       ; Save Y
                                                    65
75
61
                                                                                                                  MULD3
                                                                                                                                                                                                           RO/R1 = Y^2
                                                                                                                                      RO, #COSLENR2-1, COSTBR2: RO/R1 = Q(Y^2)
(SP)+, R6, R4 : R4/R5 = Y + YH
(SP)+, R4 : R4/R5 = YLO*(Y)
F62A CF
                                                                                                                  POLYD
                                                                                                                                                                                                           R4/R5 = Y + YHI

R4/R5 = YLO*(Y + YHI) = A2
                                                                                                                  ADDD3
                                       8Ē
05
                                                    64
                                                                                                                  MULD
                                                                                                                                                                                                     Check for A2 = 0

R4/R5 = A2/2

R0/R1 = Q(Y^2) - A2/2

R6/R7 = YHI^2

R6/R7 = YHI^2/2

R6/R7 = -(1 - YHI^2/2)
                                                                                                                  BEQL
                                                                                                                                       1$
                                                                                                                                      #*X80, R4
R4, R0
R6, R6
#*X80, R6
#1, R6
R0, R6, R0
                          0080
50
                                       8F
54
                                                    A2
64
64
63
                                                               OAE 7
                                                                               1558
                                                                                                                  SUBW
                                                               OAEC
                                                                              1559 18:
                                                                                                                  SUBD
                                      56
8F
                           56
                                                               OAEF
                                                                               1560
                                                                                                                  MULD
                          0800
                                                               OAF 2
OAF 7
             56
                                                                               1561
                                                                                                                  SUBW
                           56
56
                                                                               1562
                                        98
                                                                                                                  SUBD
             50
                                                               OAFA
                                                                                                                  SUBD3
                                                                                                                                                                                                       : RO/R1 = -DCOS(Y)
```

L 14

```
OAFE
OAFF
                             05
                                          1564
1565
                                                              RSB
              56 54
56 56
07 56
8000 8F
                                           1566 2$:
                                  OAFF
                                                                         R4, R6
R6, R6
R6, WCOSLENR1-1, COSTBR1; R0/R1 = DCOS(Y)
                                                                         R4, R6
R6, R6
                                                              ADDD
                             64
75
AC
05
                                  MULD
F5BD CF
50
                                           1568
                                                              POLYD
                                           1569
1570
                                                              XORW
                                                                         #*X8000, RO
                                                                                                           : R0/R1 = -DCOS(Y)
                                                              RSB
                                           1571
                                          1572:
1573: Polynomial evaluation for -DSIN(Y)
1574:
                                          1575
1576 N_SIN_R:
1577
1578
                                      54
56
              8000 8F
8000 8F
                            AC
AC
                                                                                                           R4/R7 = -Y
                                                                        R4, -(SP)
R4, R6, -(SP)
(SP), (SP), R4
R4, #SINLENR-1, SINTBR
(SP)+, R0
(SP)+, R0
R6, R0
              76
56
60
70
50
50
                     54
54
65
88
56
58
56
                                                                                                            : Save YLO
7E
54
F61C CF
                            61
65
75
                                                                                                              Save Y
                                           1587
                                                              MULD3
                                                                                                              R4 = Y^2
                                           1588
1589
1590
1591
1592
1593
                                                              POLYD
                                                                                                              R0/R1 = P(Y^2)
                            64
60
60
05
                                                              MULD
                                                                                                              RO/R1 = Y*P(Y^2)
                                                              ADDD
                                                                                                              R0/R1 = YLO + Y*P(Y^2)
                                                              ADDD
                                                                                                            RO/R1 = Y + Y*P(Y^2) = DSIN(Y)
                                                              RSB
                                  0B36
                                          1594
```

```
1597
1598
                                0B36
                                0836
                                       1599
                                0B36
                                        1600
                                0B36
                                        1601
                                       1602
                                0B36
                                                 Polynomial evaluation for DCOS(Y) for Y in cycles
                                0B36
                                        1604
                                       1605 P_COS_C:
                                0836
             F4EE CF
                                                                   D_2_OV_PI, R6
      56
                                0B36
                                       1606
                                                        CMPD
                                                                                                   ; Compare 2/pi with LYHIL
                                0B3B
                                       1607
                                                         BGEQ
                                                                                                     Sufficent overhang is available
             7E 4 6E 7 5 6 5 4
                                0B3D
                                                                   R4, -(SP)
                    54650
5650
8850
5650
                          7D
                                       1608
                                                         DVOM
                                                                                                     Save YLO
                                                                   R6, R4, -(SP) ; Save Y
(SP), (SP), R0 ; R0/R1 = Y^2
R0, #COSLENC2-1, COSTBC2; R0/R1 = Q(Y^2)
                          61
                                0B40
                                       1609
                                                         ADDD3
                          65
75
                                0844
                                      1610
                                                         MULD3
F67A CF
                               0B48
                                      1611
                                                         POLYD
                               084E
0852
0855
0857
085C
                                                                   (SP)+, R6, R4
                                      1612
                          61
                                                         ADDD3
                                                                                                     R4/R5 = Y + YHI
                          MULD
                                                                   (SP)+, R4
                                                                                                     R4/R5 = YL0*(Y + YHI) = A2
                                                                                                     Check for A2 = 0
R4/R5 = A2/4
                                       1614
                                                         BEQL
                                                                   1$
             0100
                   8F
54
                                                         SUBW
                                                                   #*X100, R4
                                      1615
             50
                                                                                                     R0/R1 = Q(Y^2) - A2/4

R6/R7 = YHI^2
                                      1616 1$:
                                                         SUBD
                                                                   R4, R0
             56
                    56
                                OB5F
                                      1617
                                                         MULD
                                                                   R6, R6
             0100 8F
56 08
50 56
                               0B62
0B67
0B6A
0B6D
       56
                                       1618
                                                         SUBW
                                                                   #^X100, R6
                                                                                                   : R6/R7 = YHI^2/4
                                                                                                   R6/R7 = -(1 - YHI^2/4)
                                      1619
                                                         SUBD
                                                                   #1, R6
                                      1620
                                                         SUBD
                                                                   R6, R0
                                                                                                  : RO/R1 = DCOS(Y)
                                       1621
                                                         RSB
                               086E
086E
0871
0874
087A
                                      1622
1623 2$:
1624
1625
                          60
64
75
                                                         ADDD
                                                                   R4, R6
                                                                                                     R6/R7 = Y
                    56
56
             56
                                                         MULD
                                                                   R6, R6
                                                                                                     R6/R7 = Y^2
                                                                   R6, #COSLENC1-1, COSTBC1; R0/R1 = DCOS(Y) - 1
#1, R0 : R0/R1 = DCOS(Y)
             ÓŽ
F60E CF
                                                        POLYD
                                       1626
1627
1628
1629
                          60
                                                         ADDD
                                                         RSB
                                OB7E
                                OB7E
                                      1630 ;
1631 ; Polynomial evaluation for -DCOS(Y)
                                OB7E
                                OB7E
                                OB7E
                                OB7E
                                       1633
                                OB7E
                                       1634 N_COS_C:
                               OB7E
                                                                   D_2_OV_PI, R6
2$
R4, -(SP)
                                      1635
                                                        CMPD
             F4A6 CF
                          71
      56
                                                                                                  : Compare 2/pi with :YH1:
                               0883
0885
0888
                                       1636
                                                        BGEQ
                                                                                                   ; Sufficent overhang is available
             7E
54
                          7D
                                      1637
                                                        MOVQ
                                                                                                   ; Save YLO
                                                                  R6, R4, -(SP)
(SP), (SP), R0
R0, #COSLENC2-1, COSTBC2: R0/R1 = Q(Y^2)
(SP)+, R6, R4
(SP)+, R4

R4/R5 = YLO*(Y
                   56
6E
50
8E
                          61
65
75
                                       1638
                                                        ADDD3
                               0B8C 1639
0B90 1640
             6E
                                                        MULD3
F632 CF
             Ŏ7
                                                        POLYD
             56
                          61
                               0896
                                      1641
                                                         ADDD3
                                                                                                     R4/R5 = Y + YHI
                          64
             54
                    8Ē
                                0B9A
                                       1642
                                                        MULD
                                                                                                     R4/R5 = YL0*(Y + YHI) = A2
                                                                                                     Check for A2 = 0
                    Ŏ5
                                0B9D
                                                         BEQL
                                                                   15
                          A2
62
                                                                   #^X100, R4
             0100
                   8F
                                089F
                                                         SUBW
                                       1644
                                                                                                     R4/R5 = A2/4
                                                                                                    R0/R1 = Q(Y^2) - A2/4

R6/R7 = YHI^2
             50
                                OBA4
                                                                   R4, R0
                                       1645 15:
                                                         SUBD
                          64
A2
63
             56
                    56
                                OBA7
                                                                   R6, R6
                                       1646
                                                         MULD
       56
             0100 8F
                                       1647
                                                                                                    R6/R7 = YHI^2/4

R6/R7 = -(1 - YHI^2/4)
                                OBAA
                                                         SUBW
                    08
                                                                   #1, R6
             56
                                OBAF
                                       1648
                                                         SUBD
                                                                   RO, R6, RO
       50
             56
                                0882
                                       1649
                                                                                                  : RO/R1 = -DCOS(Y)
                                                         SUBD3
                          ŎŠ
                                0BB6
                                       1650
                                                         RSB
                                0887
                                       1651
                    54
56
                                       1652 2$:
1653
                                                                   R4, R6
R6, R6
                                                                                                  : R6/R7 = Y
: R6/R7 = Y^2
                          60
                                0887
                                                         ADDD
                                OBBA
                                                         MULD
```

```
B 15
                                               ; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 PCYCLE_POLYNOMIALS; Polynomials for argu 6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1
MTH$DSINCOS
2-007
                                                75
63
05
                                         56
50
                                                      0BBD 1654
0BC3 1655
                   F5C5 CF
                                                                                              R6, #COSLENC1-1, COSTBC1; R0/R1 = DCOS(Y) - 1
R0, #-1, R0 ; R0/R1 = -DCOS(Y)
                                                                                  POLYD
       0000000 0000c080 8F
50
                                                               1655
                                                                                  SJBD3
                                                                                  RSB
                                                      OBCF
                                                               1656
                                                       OBDO
                                                              1657
                                                      OBDO 1658:
OBDO 1659: Polynomial evaluation for -SIN(Y)
                                                       OBDO 1660 :
                                                       OBDO
                                                               1661
                                                              1662 N_SIN_C:
1663
                                                       OBDO
                          54
56
                                  8000 8F
                                                                                              #^X8000, R4
#^X8000, R6
                                                AC
AC
                                                      OBDO
                                                                                 XORW
                                                                                                                                  34/R7 = - y
                                  8000 8F
                                                      OBD 5
                                                               1664
                                                                                  XORW
                                                       OBDA
                                                               1665
                                                      OBDA 1666;
OBDA 1667; Polynomial evaluation for DSIN(Y)
                                                      OBDA
                                                               1669
                                                       OBDA
                                                               1670 P_SIN_C:
                                                                                             R4, -(SP)

R4, R6, -(SP)

(SP), (SP), R4

R4, #SINLENC-1, SINTBC

(SP)+, R0

(SP), R0

#^x100, (SP)

(SP)+, R0

R6, R4

#^x100, R4

R4, R6
                                  7E
56
                                         54
54
                                                      OBDA
OBDD
                                                                                  MOVQ
                                                               1671
                                                                                                                                  ; Save YLO
                          7E
54
                                                               1672
1673
                                                                                  ADDD3
MULD3
                                                61
                                                                                                                                  ; Save Y
                                         6E
54
                                  6E
07
                                                65
75
64
                                                      OBE 1
                                                                                                                                    R4 = Y^2
                   F61D CF
                                                                                                                                    RO/R1 = P(Y^2)
                                                      OBE 5
                                                               1674
                                                                                  POLYD
                                         ŔĖ.
                                  Š0
                                                               1675
                                                      OBEB
                                                                                  MULD
                                                                                                                                    RO/R1 = Y*P(Y^2)
                                         6E
8F
                                                60
                                                      OBEE
                                                               1676
                                                                                  ADDD
                                                                                                                                    RO/R1 = Y*P(Y^2) + YLO
                                                A2
62
7D
                                  0100
                                                               1677
                                                                                                                                   (SP) = YLO/4
RO/R1 = Y*P(Y*2) + 3/4*YLO
                          6E
                                                      0BF1
                                                                                  SUBW
                                                      OBF 6
OBF 9
                                  50
                                         8E
                                                               1678
                                                                                  SUBD
                                                                                                                                  : R4/R5 = YHI
: R4/R5 = YHI/4
: R6/R7 = 3/4*YHI
                                         56
                                                               1679
                                                                                  MOVQ
                                         8F
54
56
                                                A2
62
                          54
                                  0100
                                                      OBF C
                                                               1680
                                                                                  SUBW
                                  56
                                                      0C01
                                                                                              R4, R6
                                                               1681
                                                                                  SUBD
                                  50
                                                60
                                                      0004
                                                               1682
1683
                                                                                  ADDD
                                                                                              R6, R0
                                                                                                                                  : RO/R1 = DSIN(Y)
                                                ŎŠ
                                                      0007
                                                                                  RSB
```

```
0008 1686
0008 1687
                                                     .SBTTL DEGREE_POLYNOMIALS
                                0008
                                      1688
                                ÖČÕŠ
                                      1689 P_COS_D:
               F44C CF
37
                                ÖCÖ8
          56
                                                     CMPD
                                                              D_90_OV_PI, R6
                                      1690
                                                                                          ; Compare 90/pi with Y
                           18
                                0000
                                      1691
                                                     BGEQ
                                                                                            Double precision isn't needed
                     56
54
                56
07
                           65
75
                                OCOF
                                      1692
                                                              R6, R6, R4
                                                     MULD3
                                                                                            RO/R1 = Y^2
    F66F CF
                                      1693
                                0013
                                                              R4, #COSDLN1, COSDTB1
                                                     POLYD
                                                                                            R0/R1 = Q(Y^2)
54
     56
           00070000 8F
                           CB
                               0019
                                      1694
                                                              #^X70000, R6, R4
                                                     BICL3
                           04
                                0021
                                      1695
                                                              R5
                                                     CLRL
                                                                                            R4/R5 = YHI
                           63
                               0023
                                                              R4, R6, R2
          52
                56
                                      1696
                                                     SUBD3
                                                                                            R2 = YLO
                     54
52
                56
                           60
                                ŎČŽŽ
                                      1697
                                                              R4, R6
R2, R6
1$
                                                                                            R6/R7 = Y + YHI
                                                     ADDD
                56
                                ŎČŽA
                                      1698
                           64
                                                     MULD
                                                                                            R6/R7 = YLO*(Y + YHI) = A2
                           13
                                                                                            Check for A2 = 0
R6/R7 = A2/2^13
R0/R1 = G(Y^2) - A2/2^13
                                OC2D
                                      1699
                      05
                                                     BEQL
                                                              #^X680, R6
                           A2
          56
                0680
                     8F
                                OC2F
                                      1700
                                                     SUBW
                                0034
                50
                     56
                                      1701 15:
                                                              R6, RO
                                                     SUBD
                                0C37
                                      1702
                                                              R4. R4
                                                                                          ; R4/R5 = YHI^2
                           64
                                                     MULD
                           A2
62
62
05
                0680
                     8F
          54
                                OC3A
                                      1703
                                                     SUBW
                                                              #^X680, R4
                                                                                          ; R4/R5 = YHI^2/2^13
                      80
                54
                               0C3F
                                      1704
                                                     SUBD
                                                              #1, R4
                                                                                          R4/R5 = -(1 - YHI^2/2^13)
                50
                      54
                               0C42
0C45
                                      1705
                                                              R4. R0
                                                     SUBD
                                                                                          : RO/R1 = DCOS(Y)
                                      1706
                                                     RSB
                                      1707
                                0046
                56
                     56
                           64
13
                                      1708 2$:
                                                     MULD
                                0046
                                                                                          ; R6/R7 = Y^2
                                                              R6, R6
                     07
                               0049
                                      1709
                                                     BEQL
                                                               35
                                                                                          : Check for Y = 0
                           75
05
    F5F7 CF
                07
                      56
                               0C4B
                                                              R6, #COSDLN2, COSDTB2
                                      1710
                                                     POLYD
                                                                                        : R0/R1 = Q(Y^2)
                               0051
                                      1711
                                                     RSB
                                0C52
                                      1712
                           70
05
                               0C52
0C55
                50
                     80
                                      1713 38:
                                                     MOVD
                                                              #1, RO
                                                                                          : RO/R1 = DCOS(Y)
                                      1714
                                                     RSB
                                0C56
                                      1715
                                0056
                                      1716
                               0C56 1717 N_COS_D:
                               0056
               F3FE CF
                                     1718
                                                     CMPD
                                                              D_90_OV_PI, R6
          56
                                                                                          ; Compare 90/pi with Y
                           18
65
75
                                                              25
                                      1719
                      38
                               0C5B
                                                     BGEQ
                                                                                           Double precision isn't needed
                     56
54
                                                              R6, R6, R4
                               OC5D
                                      1720
                                                                                            R0/R1 = Y^2
          54
               56
07
                                                     MULD3
    F621 CF
                               0061
                                      1721
                                                     POLYD
                                                              R4, #COSDLN1, COSDTB1
                                                                                            RO/R1 = Q(Y^2)
                     8F
54
     56
           00070000
                           CB
                               0067
                                      1722
                                                     BICL3
                                                              #^X70000, R6, R4
                           D4
63
                               0C6F
                                      1723
                                                              R5
                                                                                            R4/R5 = YHI
                                                     CLRL
                56
56
                      54
                               0071
                                      1724
                                                              R4, R6, R2
                                                                                            R2 = YLO
          52
                                                     SUBD3
                     54
52
05
                           60
                               0075
                                      1725
                                                                                            R6/R7 = Y + YHI
                                                     ADDD
                                                              R4, R6
                                                              R2. R6
                           64
                56
                               0078
                                      1726
                                                     MULD
                                                                                            R6/R7 = YL0*(Y + YHI) = A2
                                                                                          ; Check for A2 = 0; R6/R7 = A2/2^13
                               0C7B
                                      1727
                                                     BEQL
                                                              15
                           A2
62
64
                                                              ₩^X680, R6
               0680
                     8F
                               0C7D
          56
                                      1728
                                                     SUBW
                     56
54
                               0C82
0C85
                                      1729 1$: 1730
                                                                                           R0/R1 = Q(Y^2) - A2/2^13

R4/R5 = YH1^2
                                                              R6, R0
R4, R4
                50
                                                     SUBD
                54
                                                     MULD
                           A2
62
63
                                                                                          R4/R5 = YHI^2/2^13
                                                              #^X680, R4
          54
                0680
                     8F
                               8800
                                      1731
                                                     SUBW
                                      1732
1733
                                                              #1, R4
RO, R4, RO
                      80
                               0830
                                                                                           R4/R5 = -(1 - YHI^2/2^13)
                54
                                                     SUBD
                54
          50
                     50
                               0090
                                                                                          : RO/R1 = -DCOS(Y)
                                                     SUBD3
                           05
                               0094
                                      1734
                                                     RSB
                                0095
                                      1735
                           64
13
75
                56
                     56
                                0095
                                      1736 28:
                                                     MULD
                                                              R6, R6
                                                                                          : R6/R7 = Y^2
                                                                                          : Check for Y = 0
                     00
                               0098
                                      1737
                                                     BEQL
                                                              35
                                                              R6, #COSDLN2, COSDTB2
                      56
                               0C9A
                                      1738
                                                     POLYD
                                                                                           RO/R1 = DCGSD(Y)
    F5A8 CF
                8000 8F
                                      1739
                           AC
                                0CA0
                                                     XORW
                                                              #^x8000, RO
                                                                                          : RO/R1 = -DCOSD(Y)
                           05
                               OCA5
                                      1740
                                                     RSB
                                0CA6
                                      1741
 00000000 0000C080 8F
                           70 OCA6
                                      1742 38:
                                                     MOVD
                                                              #-1, RO
                                                                                         : RO/R1 = DCOS(Y)
```

5				; Fl DEGR	oating EE_POL	Point YNOMIA	Sine, LS	Cosine	and	) 15 Sinco	s 16-	SEP-1984 SEP-1984	01:20:38 11:22:35	VAX/VMS [MTHRTL	S Macro VO4-OO SRC]MTHDSINCO.MAR;1	Page	<b>39</b> (24)
				05	0CB1 0CB2 0CB2	1743 1744 1745	N_SIN_[	RSB									
		56	56	72	OCB2	1746	P_SIN_(	MNEGD	Ré	5. R6			; R6/R	7 = <b>-</b> Y			
	50	56	56 11	65 13	0CB2 0CB5 0CB5 0CB9	1748 1749		MULD3	Ré	R6,	RO		; RO/R	1 = Y^2			
F607	CF	07 50	50 56 8F	75	OCBB OCC1	1750		MULD3 BEQL POLYD MULD	R(	). #51	NDLN,	SINDTB	: RO/R : RO/R	1 = P(Y' 1 = Y*P	^2) (*^2)		
	56	6300 50	8F 56	64 60 05	0004 0009 0000 0000	1751 1752 1753 1754 1755	RETURN	ADDD	Ré	X300, X300, X, RO	R6		; R6/R ; R0/R	7 = Y/2'	<b>^</b> 6		

MTHSDSINCOS 2-007

MT Sy

DDD DDD DEGET CTTTTT MAN OPCA

MTHSDSINCOS 2-007		E 15 e, Cosine and Sincos 1	5-SEP-1984 01:20:38 VAX/VMS Macro V04-00 Page 40 5-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR;1 (26)
	OCCD 1757 OCCD 1758 OCCD 1759 OCCD 1760 OCCD 1761 P_ONE	.SBTTL DEGENERATE	SOLUTIONS
50 08	05 0CD0 1763 0CD1 1764 0CD1 1765	MOVD #1, RO RSB	; Answer is 1
50 00000000 0000C080 8F	0CD1 1766 N_ONE 70 0CD1 1767 05 0CDC 1768 0CDD 1769	: MOVD #-1, RO RSB	; Answer is -1
	0CDD 1770 0CDD 1771 UNFL: 0CDD 1772; 0CDD 1773; Und 0CDD 1774;		J set, signal error. Always return 0.0
00000000°GF 00 04 50 52 04 AD 50	DC OCDD 1775 FB OCDF 1776 E9 OCE& 1777 3C OCE9 1778 D4 OCED 1779 10\$:	BLBC RO, 10\$	; R2 = user's or jacket routine's PSL  BJACKET_TST
0D 52 06 6E 7E 00'8F	0CEF 1780 0CEF 1781 E1 0CEF 1782 GD 0CF3 1783 9A 0CF5 1784	BBC #6, R2, 209 PUSHL (SP) MOVZBL #MTH\$K_FL09	; CHPSL_MCH_RU/RT so any handler can ; fixup ; has user enabled floating underflow? ; yes, return PC from special routine JNDMAT, -(SP) ; trap code for hardware floating
0000000°GF 02	0CF9 1786 FB 0CF9 1787 05 0D00 1788 20\$: 0D01 1789	CALLS #2, G^MTH\$	underflow convert to MTH\$_FLOUNDMAT : (32-bit VAX-11 exception code) SSIGNAL ; signal (condition, PC) ; return
	0001 1790	.END	

SINE

\*\*\*\*\*\* X

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ÕÕ

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SINLENC

SINLENR

SINTBC

= 00000008 = 00000008

= 00000008

00000208 R

02

MTHSSJACKET\_HND MTHSSJACKET\_TST MTHSSSIGNAL

MTHSAL\_4\_OV\_PI

VA

Ma

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\_\$

0

Th

MA

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G 15
MTHSDSINCOS
                                      ; Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00
                                                                                                                                                  Page 42
Symbol table
                                                                                        6-SEP-1984 11:22:35 [MTHRTL.SRC]MTHDSINCO.MAR:1
SINTBR
                                       00000148 R
                                                         00000549 R
SMALL_COS
SMALL_COSD
                                       00000689 R
                                       000004CE R
000003DF R
SMALLISIN
SMALL SINCOS
SMALL SINCOSD
SMALL SIND
                                       000005E6 R
00000637 R
SUBTRACT
                                       000006C8 R
UNFL
                                       00000CDD R
W ADJUST
                                     = 00000039
W MAX WEIGHT
                                     = 00004000
W_TERM_WEIGHT
                                     = 00001000
                                     = 00000004
x_1_0v_45
                                     = 0000000B
                                                           Psect synopsis!
PSECT name
                                      Allocation
                                                              PSECT No.
                                                                           Attributes
                                                                           NOPIC
  ABS
                                      00000000
                                                        0.)
                                                              00 (
                                                                     0.)
                                                                                    USR
                                                                                           CON
                                                                                                   ABS
                                                                                                          LCL NOSHR NOEXE NORD
                                                                                                                                    NUWRT NOVEC BYTE
SABSS
                                                        0.)
                                                              Ŏ1 ( 1.)
                                      00000000
                                                                           NOPIC
                                                                                    USR
                                                                                           CON
                                                                                                   ABS
                                                                                                          LCL NOSHR
                                                                                                                       EXE
                                                                                                                               RD
                                                                                                                                      WRT NOVEC BYTE
                                                                     2.)
_MTH$CODE
                                      00000D01 (3329.)
                                                              02 (
                                                                                    USR
                                                                                           CON
                                                                                                   REL
                                                                                                          LCL
                                                                                                                 SHR
                                                                                                                        EXE
                                                                                                                                   NOWRT NOVEC LONG
                                                        Performance indicators !
Phase
                              Page faults
                                                CPU Time
                                                                 Elapsed Time
Initialization
                                       35
                                                00:00:00.08
                                                                 00:00:00.59
Command processing
                                                00:00:00.68
                                                                 00:00:03.34
                                      116
                                               00:00:05.92
00:00:00.27
Pass 1
                                      206
                                                                 00:00:18.17
Symbol table sort
                                        0
                                                                 00:00:00.42
Pass 2
                                      320
                                                00:00:03.90
                                                                 00:00:13.87
Symbol table output
                                       15
                                                00:00:00.14
                                                                 00:00:00.60
Psect synopsis output
                                        3
                                                00:00:00.02
                                                                 00:00:00.02
Cross-reference output
                                                00:00:00.00
                                                                 00:00:00.00
Assembler run totals
                                                00:00:11.02
                                                                 00:00:37.02
The working set limit was 1650 pages.
38842 bytes (76 pages) of virtual memory were used to buffer the intermediate code. There were 20 pages of symbol table space allocated to hold 194 non-local and 57 local symbols. 1850 source lines were read in Pass 1, producing 35 object records in Pass 2.
10 pages of virtual memory were used to define 9 macros.
                                                       Macro library statistics !
```

Macro Library name

Macros defined

\_\$255\$DUA28:[SYSLIB]STARLET.MLB;2

5

131 GETS were required to define 5 macros.

H 15
HTH\$D\$INCOS
Floating Point Sine, Cosine and Sincos 16-SEP-1984 01:20:38 VAX/VMS Macro V04-00 Page 43
VAX-11 Macro Run Statistics
Page 43
(26)

T a

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL, TRACEBACK)/LIS=LIS\$:MTHDSINCO/OBJ=OBJ\$:MTHDSINCO MSRC\$:MTHJACKET/UPDATE=(ENH\$:MTHJACKET)+MS

0259 AH-BT13A-SE

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